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A STUDY INTO THE DAMAGE  
TO RECTANGULAR PLATES SUBJECTED TO  
DYNAMIC LOADS  
by  
TEVFIK O. URAN



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A STUDY INTO THE DAMAGE TO  
RECTANGULAR PLATES SUBJECTED TO DYNAMIC LOADS

by

TEVFIK O. URAN  
//

B.Sc. N.A. Naval Academy, Istanbul, Turkey  
1964

SUBMITTED IN PARTIAL FULFILLMENT

OF THE REQUIREMENTS FOR THE

DEGREE OF MASTER OF

SCIENCE *[in Naval Arch. & Marine Eng.]*

at the

MASSACHUSETTS INSTITUTE OF

TECHNOLOGY

May, 1969

PS ARCHIVE

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RAN, T.

~~Thesis~~  
~~44~~

### ACKNOWLEDGEMENTS

I wish to express my appreciation to those people and institutions which have been associated with the research leading to this thesis.

Much credit is due to Professor Norman Jones. His gracious acceptance of supervision, his careful and conscientious scrutiny of the work in its several stages is proof of a rare and discriminate dedication.

Credit is due to Captain D.A. Horn, Professor of Naval Science and Naval Architecture, and Commander S.C. Reed, Associate Professor of Naval Architecture, for their support in providing the Dupont detasheet explosives and being helpful in various other stages of this work.

The thesis is based on the experimentation done in the Aeroelastic Laboratory; the use of this facility, made possible by Dr. John W. Leech, is gratefully acknowledged.

Whatever credit is my own, it pertains to my wife, Leyla.



A STUDY INTO THE DAMAGE TO RECTANGULAR  
PLATES SUBJECTED TO DYNAMIC LOADS

by

Tevfik O. Uran

Submitted to the Department of Naval Architecture and Marine Engineering on May 23, 1969 in partial fulfillment of the requirement for the degree of Master of Science in Naval Architecture and Marine Engineering.

ABSTRACT

The objective of this experimental investigation is an attempt to examine technical problems which exist due to our lack of knowledge about the accuracy of plasticity theory when applied to dynamic problems in Naval Engineering. Plastic deformation is a composite function of the physical properties of a specimen, strain-rate, strain hardening, geometry changes, etc.; and few studies have been done in this general area. An investigation of rectangular plates under uniformly distributed impulsive loading is the primary objective of this thesis and is undertaken to provide essential formation required for the development of approximate theories and design methods.

The relation of this work to Naval Engineering is clear: we will achieve improved understanding of the behavior of plates in response to grounding, slamming and underwater damages to the ship.

Since Rigid-Plastic Theory has not yet been applied to rectangular plates this study may be a tool in development of a new and simpler method in solving the rectangular plate problem.

Thesis Advisor : Norman Jones

Title : Assistant Professor of Naval Architecture







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# NOMENCLATURE

|                |   |  |   |  |
|----------------|---|--|---|--|
| $\sigma_y$     | = | Yield stress (psi)   | = | $\sigma_o$                             |
| E              | = | Young's modulus  |   |  |
| $\lambda$      | = | $\frac{\rho V_o^2 L_o^2}{\sigma_o H^2}$  | = | $\frac{\mu V_o^2 L_o^2}{\sigma_o H^3}$ |
| $\rho$         | = | 0.098 lb/in <sup>3</sup>   | = | density                                |
| $V_o$          | = | Initial velocity (ft/sec)  |   |  |
| L              | = | Shorter side of the plate  | = | 3.0 inches                             |
| H              | = | Thickness of plate (inches)  |   |  |
| $w_{max}$      | = | Maximum deflection of plate (inch)   |   |  |
| $\mu$          | = | $\rho H$   |   |  |
| w              | = | Deflection of plate (inches)   |   |  |
| $\delta_{max}$ | = | Maximum amplitude of pendulum swing  |   |  |
| N              | = | Number of cycles of pendulum swing   |   |  |
| $I_1$          | = | Moment of inertia of the specimen  | = | $m_1 D^2$                              |
| $I_2$          | = | Moment of inertia of the pendulum  |   |  |
| D              | = | Perpendicular distance from center of gravity of plate to the suspension point |   |  |
| $\bar{d}$      | = | Perpendicular distance from center of gravity of pendulum and plate            |   |  |
| g              | = | Acceleration of gravity  |   |  |
| $\theta_m$     | = | Maximum angular deflection of the pendulum                                     |   |  |
| $\omega$       | = | Angular velocity of the pendulum   |   |  |
| $m_1$          | = | Mass of specimen   |   |  |
| $m_2$          | = | Mass of pendulum   |   |  |

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## INTRODUCTION

In this study the response of thin aluminum rectangular plates subjected to laterally applied dynamic loads is examined and experimental results are developed.

In some problems in which exact solutions are known, full allowance can be made for the elastic component of strain in the plastic region. However, more complex and realistic shapes of plates enforce the necessity for the development of approximate methods. Rigid-plastic theory has been used to analyze these complex problems. In the problem of four edges clamped rectangular plate, we are compelled with mathematical difficulties to disregard the elastic component of strain. For consistency, we must also disregard the purely elastic component of strain in the non-plastic region. In effect, therefore, we work with a material that is rigid when stressed below the yield point and in which Young's modulus has an infinitely great value. This hypothetical solid may be referred to as a plastic rigid material. In many technological forming processes (e.g. rolling, drawing, forging) experience shows that the assumption of a plastic-rigid material does not lead to any significant errors.<sup>[1]</sup>

Rigid-plastic theory has been used to analyze cantilevers,<sup>[2],[3]</sup> beams,<sup>[4],[5]</sup> circular,<sup>[6]</sup> annular,<sup>[7]</sup> and square<sup>[8]</sup> plates under





dynamic loads. Rigid-plastic analyses are simple because complex elastic-plastic behavior is ignored and replaced by perfectly plastic behavior. Experiments done on beams, cantilevers, circular, and annular plates indicate that Rigid-Plastic Theory is very accurate. It is possible to extend these theories to include the influence of finite deflections. Studies on annular plates indicate when the membrane effect is dominant the influence of axial restraints are much greater than material strain-rate sensitivity. Therefore, in such situations, strain-rate sensitivity effects can be disregarded which allows simpler solutions to be obtained.

For rectangular plates an exact Rigid-Plastic solution does not exist. The closest upper and lower bounds have been achieved by Wood<sup>[9]</sup> for static loads. Cox and Morland have solved the particular case of a simply-supported square plate loaded dynamically.

To the author's knowledge no previous studies have been undertaken on the behavior of rectangular plates subjected to dynamic loads sufficient to cause large permanent deformations. In view of this and knowing that the analytical work of rectangular plates would be very complex, it is clear, that approximate methods must be developed in order to analyze more complex and realistic shapes of plates.



The author remains hopeful that the results obtained from this study will be useful in development of a new method in solving the rectangular plate problem.



### EXPERIMENTAL DETAILS

The tests reported in this thesis were carried out in the M.I.T. Aeroelastic and Structures Research Laboratory (Building 37-094). The ballistic pendulum shown in Figures 1 and 2 is attached to hinges on rails which in turn are clamped to the ceiling. Lead ballasts with different sizes were used in order to balance the pendulum and give the greatest allowable swing for each test.

In these tests Dupont Detasheet-D explosive and Dupont No.6 blasting capsules are used. Dimensions of the leader differed from test to test but the usual size was 1/8 inch by 12-20 inches.

A heat-sensitive-paper device was used in order to determine the amount of energy imparted to the pendulum. Heat-sensitive-paper is placed on the slightly curved surface of the device and a thin steel wire just touching the heat-sensitive-paper is attached to the end of pendulum. The amplitude of the swing determines the amount of energy imparted on the pendulum.

Specimens 8 inches by 6 inches were cut by band-saw and 8 holes were drilled in each specimen to provide the four edges clamped boundary condition (Figure 3). High strength steel bolts, nuts and washers were used to clamp the specimen on the head of





the pendulum. Grinding and polishing of the specimens were done manually making use of Silicon Carbide Papers (No. 240, 400, 600A and Crocus Cloth). A few drops of paraffin were applied on the specimen surface before the process to increase the cutting effect of silicon carbide paper.

In order to eliminate spalling, plastic waves, possible changes in material properties, high peak pressures in shock waves and spread of pressure waves (Appendix A) two methods were used. During the first few experiments a layer of 1/8 inch thick neoprene (weighing 42 grams with dimensions of 3 by 5 inches) was glued on the specimens underneath the explosive. Later this method was replaced with the fear that initial velocity might change due to the comparatively heavy neoprene. Foam rubber was cut (again having dimensions of 3 by 5 inches but weighing only 6 grams) and glued to the surface of each specimen underneath the explosive. Two layers of masking tape were attached to the side of the foam rubber facing the specimen in an attempt to obviate pitted surfaces on the specimen after explosion.

To increase the fixity of clamps serrations were machined on facing sides of the head (Figure 4).

To determine the actual (final) thicknesses of specimens after the polishing process fifteen readings, one inch apart from each other, from different locations on the plate were taken with



a micrometer. Percentage variation in thicknesses was found to be very small (0.25%). The average of these readings was accepted as the final thickness. Each specimen was weighed before each test and these weights are listed in Table 3.

The apparatus used in this project was prepared jointly by individuals\* who did some dynamic experiments in the general program.

In this study Al 6061-T6 is used as specimen material. Chemical and Tensile tests (Tables 1 and 2) were done at M.I.T. to have full knowledge of the chemical and mechanical properties of the material.

The formula for initial velocity of the pendulum is derived from the conservation of energy and momentum considerations and initial velocity is determined using a computer program. (Appendix C and D).

---

\*The author; Sedat Tekin, LTJG, Turkish Navy; Roger Van Duzer, LT, USN; Robert Griffin, LT, USN.



### EXPERIMENTAL DESCRIPTION AND DISCUSSION OF RESULTS

Experimental results (Table 3) show that deformed plates tend to have shapes similar to those of static collapse as shown in Figures 5 a-g and Table 4. The plates after deflection have a shape approximately of a pyramid.

For three different thicknesses of plates the relations between maximum deflections and initial velocity are plotted in Figure 6. (The formula for initial velocity is derived in Appendix C.) Differences in individual results may be due to unisotropic characteristics of the specimens. The unisotropy may arise from the different cutting locations of specimen on the Aluminum 6061-T6 sheet (Figure 7).

Nondimensionalized relation,  $w_{\max}/H$  vs  $\lambda$  (Figure 8) shows that there is no evidence of shifting in the plot between different thicknesses. Therefore, it is evident that the strain-hardening has no effect in the character of the plot. Furthermore, aluminum is believed to be strain rate insensitive. Non-linear maximum deflection/ $H - \lambda$  relation is obtained for rectangular plates. When this result is compared to linear relation of square plates and the expected linear relation to rectangular plates the influence of the membrane effects in



rectangular plates becomes obvious.

Tests done with neoprene as energy absorber are closely related to those done with foam rubber. Since the difference between two results are consistent and negligibly small no considerable error is detected when either method is used.

No theoretical comparison with the experimental results is available since there is no existing pertinent theory. Cox and Morland only considered the case of a square plate and there does not appear to be a straightforward way to extend this analysis to examine rectangular plates.





### CONCLUSIONS

An experimental study of the dynamic behavior of rectangular aluminum plates with four edges clamped and subjected to uniformly distributed impulses is presented in this thesis.

Tests have been done on rectangular Aluminum (6061-T6) plates with three different thicknesses. Deformations were measured (Table 4) and different relations were plotted on various graphs. From the results of tests done with neoprene and foam rubber as energy absorbers it is concluded that either material can be used for this purpose since neoprene bounces off after detonation just before the swing of pendulum starts, thus not affecting the initial velocity.

Results of this work should assist one in developing approximate analytical procedure to describe the behavior of rectangular plates.



## APPENDIX A

A STUDY ON NEOPRENE AS AN ENERGY ABSORBER

Subjecting plates to impulsive loads may involve the action of spalling, plastic waves, the spread of pressure waves and high peak pressures in shock waves.<sup>[11]</sup> The effects of these actions are undesirable for sound investigations of finite deflections of plates. In order to prevent these influences some means of energy absorbtion is necessary. To be able to have a full understanding of the amount of energy dissipated by the material used and the effects of this dissipation on experimental results are essential. This study is an attempt to idealize a model to give better understanding of the importance of using an energy absorber in experiments done on plates subjected to dynamic loads.

In this study a NEOPRENE layer of 1/8 inch thick is idealized as a model. An experiment done without neoprene showed that the above mentioned various actions caused the destruction of the specimen whereas when the neoprene was used desirable deflections were obtained. From these experiments it is concluded that a considerable amount of incident pressure has been reflected by the neoprene while the rest was transmitted to the specimen. To find a relation between the transmitted, reflected and incident energies let us consider the following mathematical analysis:



Initial velocity =  $u_0$

$\rho_0$  = density of air

Explosive cross section area =  $A$   $c_0$  = sound velocity in air

Mass of explosive =  $M$

$u$  = particle velocity

$t$  = time

Assume explosion hits neoprene at  $t = 0$ ,

for plane waves we have  $p = \rho_0 c_0 u_0$  - pressure in surface layer  
of neoprene

at time " $t$ " velocity of explosive waves is  $u(t)$  and pressure

at neoprene surface is  $p(t) = \rho_0 c_0 u$ .

Differential equation, before the stress wave hits steel plate, is: [12]

$$M \frac{du}{dt} + p(t) A = 0$$

$$M \frac{du}{dt} = - \rho_0 c_0 u A$$

$$\frac{du}{u} = - \frac{\rho_0 c_0 A}{M} dt$$

$$\log u = - \frac{\rho_0 c_0 A}{M} t + B$$

Boundary condition  $\rightarrow u = u_0$  at  $t = 0 \Rightarrow B = \log u_0$

$$\therefore \log u = - \frac{\rho_0 c_0 A}{M} t + \log u_0$$

$$\log \left( \frac{u}{u_0} \right) = - \frac{\rho_0 c_0 A}{M} t$$

$$\frac{u}{u_0} = e^{- \frac{\rho_0 c_0 A}{M} t}$$





$$u = u_o e^{-\frac{\rho_o c_o A}{M} t}$$

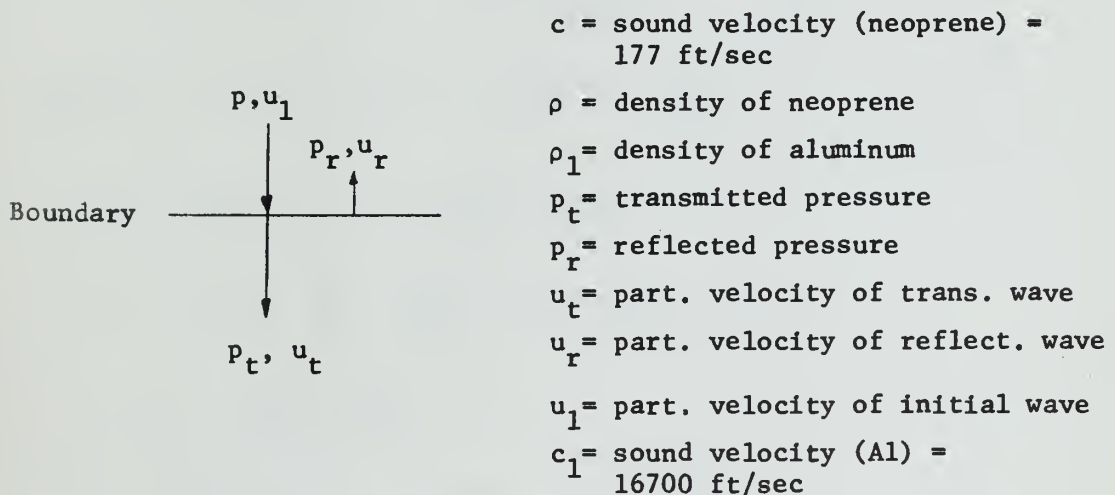
$$\text{But } p = \rho_o c_o u$$

$$\therefore p = \rho_o c_o u_o e^{-\frac{\rho_o c_o A}{M} t} \quad \text{or } p = p_o e^{-t/Q}$$

$$\text{where, } p_o = \rho_o c_o u_o \quad \text{and } Q = \frac{M}{\rho_o c_o A}$$

This equation represents the time history of pressure wave travelling along neoprene.

Now let us consider the clamped condition between neoprene and plate at which the pressure wave reaches the neoprene-aluminum boundary:



for continuous displacement and velocity at the boundary, we have:

$$u_r = -(u_t - u_1) \quad (1)$$

$$\text{From force eqn at the boundary } = p + p_r = p_t \quad (2)$$



We also have  $p = \rho c u_1$  (3)

$$p_t = \rho_1 c_1 u_t \quad (4)$$

$$p_r = \rho c u_r \quad (5)$$

$p$  and  $u_1$  are known for the incident while  $u_t$ ,  $p_t$ ,  $u_r$ ,  $p_r$  remain to be found.

$$\begin{aligned} \text{From (1)} \quad u_r &= u_1 - u_t \\ u_r &= \frac{p_r}{\rho c} \end{aligned} \quad \} \Rightarrow \quad u_1 - u_t = \frac{p_r}{\rho c}$$

$$u_t = u_1 - \frac{p_r}{\rho c} \quad (6)$$

$$\begin{aligned} \text{From (2)} \quad p_t &= p + p_r \\ \text{From (4)} \quad p_t &= \rho_1 c_1 u_t \end{aligned} \quad \} \quad p + p_r = \rho_1 c_1 u_t$$

$$u_t = \frac{p + p_r}{\rho_1 c_1} \quad (7)$$

$$\text{Combine (6) and (7)} \quad u_t = u_1 - \frac{p_r}{\rho c} = \frac{p + p_r}{\rho_1 c_1}$$

$$u_1 - \frac{p}{\rho_1 c_1} = p_r \left( \frac{1}{\rho_1 c_1} + \frac{1}{\rho c} \right)$$

$$u_1 = \frac{p}{\rho c} \Rightarrow \frac{p}{\rho c} - \frac{p}{\rho_1 c_1} = p_r \left( \frac{1}{\rho_1 c_1} + \frac{1}{\rho c} \right)$$

$$p_r = p \left( \frac{\rho_1 c_1 - \rho c}{\rho_1 c_1 + \rho c} \right)$$

$$\text{Let } \epsilon = \frac{\rho c}{\rho_1 c_1} \quad \text{Then } p_r = p \left( \frac{1 - \epsilon}{1 + \epsilon} \right)$$

$$\text{Now } p_t = p + p_r$$



$$p_t = p \left[ 1 + \left( \frac{\rho_1 c_1 - \rho c}{\rho_1 c_1 + \rho c} \right) \right] = p \left( \frac{\rho_1 c_1 + \rho c + \rho_1 c_1 - \rho c}{\rho_1 c_1 + \rho c} \right)$$

$$p_t = p \left( \frac{2 \rho_1 c_1}{\rho_1 c_1 + \rho c} \right)$$

$$p_t = p \left( \frac{2}{1+\epsilon} \right)$$

There is no change of time history of the waves at such reflections.

$$\begin{aligned} \text{Since } \epsilon &= \frac{\rho c}{\rho_1 c_1} \quad \text{where} \quad \rho = 0.098 \text{ lb/ft}^3 \\ &\quad \rho_1 = 0.04 \text{ lb/ft}^3 \\ \epsilon &= \frac{0.098 * 16700}{177 * 0.04} = 231 \quad c = 16700 \text{ ft/sec} \\ &\quad c_1 = 177 \text{ ft/sec} \end{aligned}$$

$$\therefore p_t = p \left( \frac{2}{232} \right) = .009 p$$

which shows a great reduction in pressure wave. This simplified calculation of transmitted pressure wave proves that the influence of neoprene in impulsively loaded plate tests is of great importance. Therefore, we must use neoprene or some other substances (e.g. foam rubber) in order not to damage the testing specimens.



## APPENDIX B

WEIGHT ESTIMATION

Pendulum = 44.814 lb.

Head a. Explosive face 5160 grams

b. Pendulum face 5125 grams

Lead Ballasts #1 1815 grams

#2 1780 grams

#3 3205 grams

#4 2099 grams

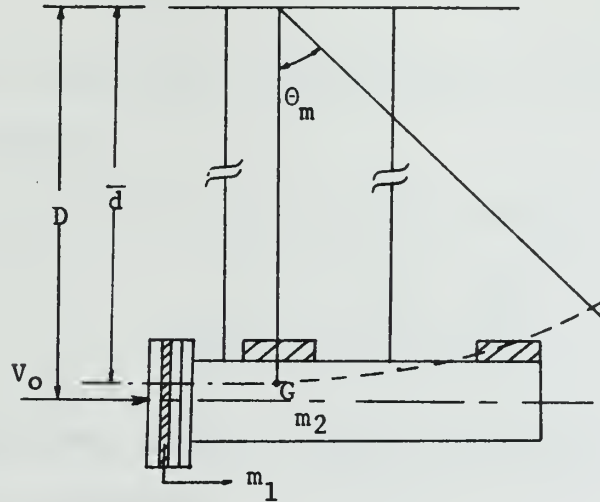
4 Steel Supports = 750 grams (see Figure 4)  
(between head and pendulum)

Height of pendulum from ground to hinges = 11 ft. 6 in.





## APPENDIX C

DETERMINATION OF INITIAL VELOCITY OF THE PENDULUM<sup>[10]</sup>

A combination of direct and rotational impulse occurs in the use of the ballistic pendulum. When the detasheet explosive is detonated it initiates rotation of the pendulum. The observed amplitude of this motion can then be used to calculate the initial velocity  $V_0$ . If  $D$  is the perpendicular distance from center of gravity of plate to the suspension point,  $\theta_m$  the maximum angular deflection of the pendulum and  $\omega$  is it's angular velocity immediately after impulse, and if  $m_1$ ,  $m_2$ , and  $I_1 = m_1 D^2$ ,  $I_2$  represent the masses and moments of inertia about the pivot of the specimen and pendulum respectively then,



$$I_2 \omega = D m_1 (V_o - D \omega) \quad (1-a)$$

$$V_o = \frac{I_2 + m_1 D^2}{m_1 D} \omega \quad (1-b)$$

The law of conservation of energy applied to this process yields the relation

$$\begin{aligned} \frac{1}{2} [ I_2 + m_1 D^2 ] \omega^2 &= g (m_1 + m_2) \bar{d} (1 - \cos \theta_m) \\ &= 2g (m_1 + m_2) \bar{d} \sin \frac{\theta_m}{2} \end{aligned} \quad (2)$$

where  $\bar{d}$  is the distance from the center of gravity of pendulum and specimen to the support.

Substitution of Equation (2) in Equation (1-b) determines the initial velocity  $V_o$  as

$$V_o = \frac{\sqrt{2g(I_2 + m_1 D^2) \bar{d} (1 - \cos \theta_m) (m_1 + m_2)}}{m_1 D}$$

$$\text{or } V_o \approx \left( \frac{2}{m_1} \right) \left( \sin \frac{\theta_m}{2} \right) \sqrt{(g I_2 m_2) / D}$$

when  $\bar{d} \approx D$  and  $m_1 \ll m_2$

A computer program was written using Equation (3) to evaluate the initial velocity for each test and the results are presented in Appendix D.



## APPENDIX D

COMPUTER PROGRAM TO CALCULATE V

FORTRAN IV G LEVEL 1, MOD 3      MAIN      DATE= 19/10/06      PAGE 0001

```

100  FORMAT(7F10.2)
300  FORMAT(5X,'E=',F10.5,2X,'A=',F10.5,2X,'W=',F10.5,2X,'V=',F20.5)
10   READ(5,100)BER,B,ASS,TL,Y,BH,TH
      BTA=TL/133.425
      Z=ASS+B+29431.887
      CG=((Z-B)*2.4875+B*5.975)/Z
      X=TH*BH*44.814*5.0625
      D=138.8-Y-CG
      BL=136.3125-Y
      ERT=X*BL**2.
      ERTB=Z*D**2.
      AA=SQRT(772.08*(ERTB+ERT)*D*(1.-COS(BTA))*(X+Z))
      V=AA/(X*BL*12.0)
      WRITE(6,300)VER,BTA,X,V
      IF(BER.NE.0.0)GO TO 10
      CONTINUE
      RETURN
      END

```

|           |            |              |              |
|-----------|------------|--------------|--------------|
| E= III 14 | A= 0.03232 | W= 127.81900 | V= 183.01584 |
| E= III 1  | A= 0.04591 | W= 128.02316 | V= 259.71631 |
| E= II 14  | A= 0.03841 | W= 83.71524  | V= 330.42529 |
| E= II 1   | A= 0.03092 | W= 83.10275  | V= 267.95264 |
| E= III 15 | A= 0.06980 | W= 127.95511 | V= 395.32813 |
| E= III 16 | A= 0.07401 | W= 128.22734 | V= 417.87256 |
| E= III 12 | A= 0.04075 | W= 127.68282 | V= 226.56285 |
| E= III 17 | A= 0.03466 | W= 127.88698 | V= 176.96474 |
| E= III 24 | A= 0.07307 | W= 128.33626 | V= 412.40063 |
| E= III 22 | A= 0.03584 | W= 128.65613 | V= 201.57072 |
| E= IV 1   | A= 0.04731 | W= 166.35529 | V= 190.44037 |
| E= IV 2   | A= 0.03701 | W= 166.38248 | V= 148.92992 |
| E= IV 8   | A= 0.07214 | W= 166.38248 | V= 331.59277 |
| E= IV 4   | A= 0.07542 | W= 166.20551 | V= 346.88477 |
| E= IV 5   | A= 0.06464 | W= 166.41655 | V= 297.13306 |
| E= IV 7   | A= 0.06839 | W= 166.38248 | V= 275.29224 |
| E= II 12  | A= 0.02928 | W= 83.10275  | V= 251.86386 |
| E= II 17  | A= 0.04591 | W= 83.91949  | V= 389.20361 |
| E= II 15  | A= 0.02717 | W= 83.57913  | V= 230.99631 |



|           |            |              |              |
|-----------|------------|--------------|--------------|
| E= III 13 | A= 0.03185 | W= 128.15927 | V= 180.02188 |
| E= I 14   | A= 0.03118 | W= 60.77867  | V= 368.09546 |
| E= I 1    | A= 0.03876 | W= 60.43835  | V= 459.72339 |
| E= II 13  | A= 0.04684 | W= 83.23886  | V= 405.02759 |
| E= I 2    | A= 0.03185 | W= 60.84676  | V= 375.71802 |

Where, E = Specimen number

A = Angle pendulum swing (radians)

W = Weight of target plate (grams)

V =  $V_o$  (ft/sec)

and

I - .089 in plate

II - .1225 in plate

III - .189 in plate

IV - .244 in plate





TABLE 1

REPORT OF CHEMICAL ANALYSIS

Description of Samples: Al 6061 - T6

| SAMPLE   | % Si | % Cu | % Mg  | % Cr |
|----------|------|------|-------|------|
| 11/.1225 | 0.65 | 0.20 | 0.85  | 0.26 |
| 11/.189  | 0.61 | 0.21 | 0.83  | 0.21 |
| 13/.089  | 0.57 | 0.24 | 0.89  | 0.23 |
| .25      | 0.60 | 0.24 | 1.04* | 0.17 |

\* Examination of the chemical-test results shows a percentage increase of magnesium in the composition of 0.244 inch thick plates. However, Al 6061-T6 may contain a maximum of 1.20% magnesium without the mechanical properties of the alloy being changed<sup>[13]</sup>. The chemical test for the plates of different thicknesses are found to lie under this limit resulting with the fact that the plates used in the experiments have the same mechanical behavior (i.e. same elongation, hardness, fatigue endurance limit and work hardening in annealed or solution-heat-treated condition.<sup>[14]</sup>) In conclusion, it is certain that higher percent Mg has no effect or influence on the 0.244 inch plate.



TABLE 2

TENSILE TEST RESULTS FOR 6061 - T6 ALUMINUM

All Samples 1/2 inches by 9 inches by thickness

| SAMPLE | THICKNESS | $\sigma$ yield(psi) | E(psi)           |
|--------|-----------|---------------------|------------------|
| 16     | 0.089     | 41800*              | 9.85 ( $10^6$ )  |
| 15     | .089      | 37800*              | 10.8 ( $10^6$ )  |
| 7      | .1225     | 41300               | 10.5 ( $10^6$ )  |
| 9      | .1225     | 40500               | 10.85 ( $10^6$ ) |
| 8      | .1225     | 41700               | 11.68 ( $10^6$ ) |
| 4      | .187      | 40100               | 10.75 ( $10^6$ ) |
| 6      | .189      | 41400               | 9.78 ( $10^6$ )  |
| 19     | .246      | 41500               | 10.8 ( $10^6$ )  |
| 18     | .246      | 41400               | 9.4 ( $10^6$ )   |

\* Differences in individual results may be due to unisotropy of the specimens since they are cut from different parts of the Aluminum sheets as shown in Figure 7.

The yield stress is the stress at which the material exhibits either a specified limiting deviation from the proportionality of stress to strain. When the deviation is expressed in terms of an increase in strain above the proportional value the result is termed an offset yield strength. The offset is usually specified to be 0.2% (a plastic strain of .002) for steel and aluminum alloys.<sup>[15]</sup> Therefore, in order to determine yield strength of the material used in experiments an offset of .2% is used.



TABLE 3  
BASIC INFORMATION OF EXPERIMENTAL RESULTS

| Specimen No. | Weight (gr) | H(in)  | $\delta$ (in) | $w_{\max}$ (in) | $w_{\max}/H$ (in) | $V_o$ (ft/sec) | $\lambda$ | Neoprene or Foam | Comments           |
|--------------|-------------|--------|---------------|-----------------|-------------------|----------------|-----------|------------------|--------------------|
| 1            | 575         | .24442 | 6 5/16        | .109            | .446              | 190.44037      | 12.8      | F                | O.K.               |
| 2            | 573         | .24446 | 4 15/64       | .047            | .192              | 148.92992      | 7.9       | F                | O.K.               |
| 4            | 573         | .2442  | 10 1/16       | .325            | 1.33              | 346.88477      | 42.7      | F                | O.K.               |
| 5            | 575         | .24451 | 8 5/8         | .225            | .92               | 297.13306      | 31.7      | F                | O.K.               |
| 7            | 576         | .24446 | 9 1/8         | .214            | .87               | 275.29224      | 27.1      | F                | O.K.               |
| 8            | 580         | .24446 | 9 20/32       | .297            | 1.211             | 331.59277      | 39.2      | F                | O.K.               |
| 1            | 436         | .1881  | 6 4/32        | .227            | 1.205             | 259.71631      | 41.0      | N                | Good results       |
| 12           | 438         | .1876  | 5 7/16        | .192            | 1.025             | 226.56285      | 30.6      | F                | O.K.               |
| 13           | 435         | .1883  | 6 8/32        | -               | -                 | 180.02188      | -         | without N or F   | Spalling and shear |
| 14           | 437         | .1878  | 4 10/32       | .158            | .843              | 183.01584      | 20.5      | N                | Good results       |
| 15           | 437         | .1880  | 9 5/16        | .3765           | 2.000             | 395.32813      | 95.25     | F                | O.K.               |
| 16           | 440         | .1884  | 9 7/8         | .454            | 2.41              | 417.87256      | 106.5     | F                | Shear              |
| 17           | 440         | .1879  | 4 5/8         | .151            | .805              | 176.96474      | 19.1      | F                | O.K.               |
| 22           | 444         | .18903 | 4 25/32       | .158            | .837              | 201.57072      | 24.7      | F                | O.K.               |
| 24           | 440         | .18856 | 9 3/4         | .418            | 2.22              | 412.40063      | 103.8     | F                | O.K.               |
| 1            | 278         | .1221  | 4 8/64        | .289            | 2.362             | 267.95264      | 103.0     | N                | O.K.               |



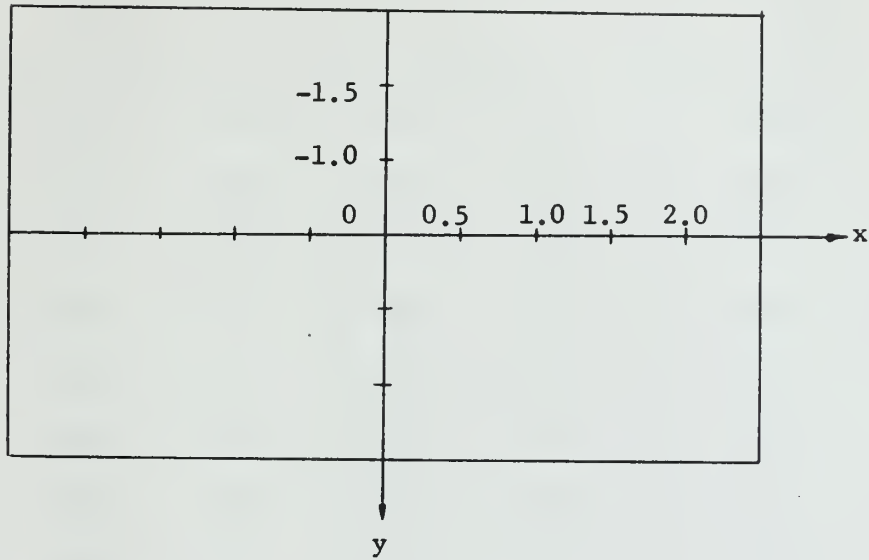
Table 3 - continued

| Specimen No. | Weight (gr) | H(in) | $\delta$ (in) | $w_{\max}$ (in) | $w_{\max}/H$ (in) | $V_o$ (ft/sec) | $\lambda$ | Neoprene or Foam | Comments                              |
|--------------|-------------|-------|---------------|-----------------|-------------------|----------------|-----------|------------------|---------------------------------------|
| 12           | 281         | .1221 | 3 29/32       | .271            | 2.205             | 251.86386      | 90.6      | F                | O.K.                                  |
| 13           | 282         | .1223 | 6 1/4         | -               | -                 | 405.02759      | -         | F                | Slipped                               |
| 14           | 281         | .1230 | 5 8/64        | .350            | 2.842             | 330.42529      | 157.0     | N                | Slightly slipped                      |
| 15           | 287         | .1228 | 3 5/8         | .222            | 1.82              | 230.99631      | 76.2      | F                | O.K.                                  |
| 16           | 281         | .1226 | 10 12/64      | -               | -                 | -              | -         | N                | Excessive charge ripped off the plate |
| 17           | 288         | .1233 | 6 1/8         | .429            | 3.48              | 389.20361      | 216       | F                | O.K.                                  |
| 1            | 182         | .0888 | 5 11/64       | -               | -                 | 459.72339      | -         | N                | Slipped                               |
| 2            | 180         | .0894 | 4 1/4         | -               | -                 | 375.71802      | -         | F                | Very slight slip                      |
| 14           | 185         | .0893 | 4 10/64       | -               | -                 | 368.09546      | -         | N                | Slipped                               |





TABLE 4

FINAL DEFORMATION OF PLATES

Specimen No. 15 Thickness = .188 inches

| $\begin{matrix} y \\ x \end{matrix}$ | -1.0  | -0.5  | 0      | 0.5   | 1.0   |
|--------------------------------------|-------|-------|--------|-------|-------|
| -2.0                                 | 0.077 | 0.134 | .145   | .130  | .078  |
| -1.5                                 | .117  | .223  | .260   | .225  | .118  |
| -1.0                                 | .140  | .264  | .3285  | .262  | .141  |
| -0.5                                 | .158  | .295  | .361   | .292  | .160  |
| 0                                    | .179  | .304  | .3765* | .305  | .175  |
| 0.5                                  | .161  | .295  | .360   | .2935 | .161  |
| 1.0                                  | .140  | .259  | .322   | .260  | .141  |
| 1.5                                  | .1195 | .221  | .258   | .219  | .1175 |
| 2.0                                  | .078  | .131  | .147   | .132  | .079  |

\* .3765 = maximum deflection of plate,  $w_{\max}$  (inches)



Table 4 - continued

Specimen No. 17 Thickness = .1879 inches

| $\begin{matrix} y \\ x \end{matrix}$ | -1.0  | -0.5  | 0     | 0.5  | 1.0   |
|--------------------------------------|-------|-------|-------|------|-------|
| -2.0                                 | .0195 | .0355 | .045  | .036 | .0195 |
| -1.5                                 | .040  | .076  | .091  | .075 | .040  |
| -1.0                                 | .05   | .097  | .123  | .097 | .052  |
| -0.5                                 | .058  | .111  | .141  | .113 | .060  |
| 0                                    | .0625 | .120  | .151* | .120 | .063  |
| 0.5                                  | .057  | .112  | .143  | .114 | .060  |
| 1.0                                  | .050  | .098  | .122  | .095 | .051  |
| 1.5                                  | .039  | .077  | .092  | .075 | .040  |
| 2.0                                  | .0215 | .039  | .046  | .040 | .023  |

Specimen No. 22 Thickness = .189 inches

| $\begin{matrix} y \\ x \end{matrix}$ | -1.0 | -0.5  | 0     | 0.5   | 1.0  |
|--------------------------------------|------|-------|-------|-------|------|
| -2.0                                 | .020 | .0415 | .047  | .045  | .022 |
| -1.5                                 | .042 | .078  | .095  | .080  | .049 |
| -1.0                                 | .056 | .103  | .127  | .110  | .064 |
| -0.5                                 | .067 | .121  | .147  | .127  | .070 |
| 0                                    | .069 | .130  | .158* | .133  | .074 |
| 0.5                                  | .067 | .123  | .150  | .1235 | .069 |
| 1.0                                  | .058 | .105  | .131  | .108  | .063 |
| 1.5                                  | .042 | .080  | .100  | .085  | .047 |
| 2.0                                  | .021 | .037  | .05   | .047  | .026 |

\*Maximum deflection



Table 4 - continued

Specimen No. 1 Thickness = .2444 inches

| $\begin{array}{c} y \\ x \end{array}$ | -1.0  | -0.5  | 0     | 0.5   | 1.0  |
|---------------------------------------|-------|-------|-------|-------|------|
| -2.0                                  | .013  | .024  | .031  | .026  | .012 |
| -1.5                                  | .026  | .0495 | .065  | .050  | .025 |
| -1.0                                  | .035  | .067  | .086  | .068  | .036 |
| -0.5                                  | .040  | .079  | .102  | .080  | .044 |
| 0                                     | .043  | .087  | .109* | .0875 | .046 |
| 0.5                                   | .040  | .080  | .104  | .082  | .045 |
| 1.0                                   | .033  | .070  | .090  | .069  | .036 |
| 1.5                                   | .024  | .052  | .069  | .056  | .026 |
| 2.0                                   | .0125 | .027  | .036  | .029  | .015 |

Specimen No. 5 Thickness = .24451 inches

| $\begin{array}{c} y \\ x \end{array}$ | -1.0  | -0.5  | 0     | 0.5   | 1.0   |
|---------------------------------------|-------|-------|-------|-------|-------|
| -2.0                                  | .032  | .056  | .0645 | .0565 | .032  |
| -1.5                                  | .058  | .1185 | .132  | .1135 | .058  |
| -1.0                                  | .079  | .149  | .179  | .143  | .076  |
| -0.5                                  | .090  | .171  | .2145 | .168  | .087  |
| 0                                     | .095  | .177  | .225* | .173  | .093  |
| 0.5                                   | .090  | .170  | .208  | .162  | .088  |
| 1.0                                   | .074  | .147  | .177  | .139  | .073  |
| 1.5                                   | .0575 | .115  | .126  | .109  | .058  |
| 2.0                                   | .0315 | .058  | .066  | .0585 | .0315 |

\*Maximum deflection



Table 4 - continued

Specimen No. 8 Thickness = .24446 inches

| $\begin{array}{c} y \\ x \end{array}$ | -1.0  | -0.5  | 0     | 0.5   | 1.0   |
|---------------------------------------|-------|-------|-------|-------|-------|
| -2.0                                  | .049  | .0765 | .093  | .078  | .0482 |
| -1.5                                  | .084  | .160  | .187  | .1602 | .090  |
| -1.0                                  | .1085 | .200  | .2465 | .203  | .110  |
| -0.5                                  | .116  | .2245 | .285  | .234  | .1308 |
| 0                                     | .121  | .233  | .297* | .2424 | .132  |
| 0.5                                   | .114  | .225  | .282  | .231  | .1305 |
| 1.0                                   | .105  | .194  | .241  | .203  | .111  |
| 1.5                                   | .0835 | .151  | .183  | .160  | .089  |
| 2.0                                   | .050  | .0785 | .096  | .081  | .051  |

Specimen No. 7 Thickness = .24446 inches

| $\begin{array}{c} y \\ x \end{array}$ | -1.0  | -0.5  | 0     | 0.5   | 1.0   |
|---------------------------------------|-------|-------|-------|-------|-------|
| -2.0                                  | .0385 | .067  | .074  | .065  | .367  |
| -1.5                                  | .072  | .123  | .140  | .1205 | .070  |
| -1.0                                  | .091  | .160  | .189  | .158  | .089  |
| -0.5                                  | .105  | .184  | .202  | .182  | .100  |
| 0                                     | .108  | .194  | .214* | .194  | .1075 |
| 0.5                                   | .105  | .185  | .204  | .182  | .101  |
| 1.0                                   | .0905 | .159  | .190  | .158  | .091  |
| 1.5                                   | .0715 | .1265 | .1425 | .121  | .0691 |
| 2.0                                   | .038  | .065  | .073  | .0648 | .039  |

\*Maximum deflection





Table 4 - continued

Specimen No. 14 Thickness = .123 inches

| $\begin{matrix} y \\ x \end{matrix}$ | -1.0 | -0.5 | 0     | 0.5  | 1.0  |
|--------------------------------------|------|------|-------|------|------|
| -2.0                                 |      |      | .157  |      |      |
| -1.5                                 |      |      | .258  |      |      |
| -1.0                                 |      |      | .317  |      |      |
| -0.5                                 |      |      | .336  |      |      |
| 0                                    | .174 |      | .350* | .297 | .177 |
| 0.5                                  |      |      | .341  |      |      |
| 1.0                                  |      |      | .320  |      |      |
| 1.5                                  |      |      | .2645 |      |      |
| 2.0                                  |      |      | .259  |      |      |

Specimen No. 1 Thickness = .1221 inches

| $\begin{matrix} y \\ x \end{matrix}$ | -1.0 | -0.5 | 0     | 0.5  | 1.0  |
|--------------------------------------|------|------|-------|------|------|
| -2.0                                 |      |      | .140  |      |      |
| -1.5                                 |      |      | .230  |      |      |
| -1.0                                 |      |      | .273  |      |      |
| -0.5                                 |      |      | .284  |      |      |
| 0                                    | .145 | .253 | .289* | .253 | .145 |
| 0.5                                  |      |      | .285  |      |      |
| 1.0                                  |      |      | .275  |      |      |
| 1.5                                  |      |      | .232  |      |      |
| 2.0                                  |      |      | .142  |      |      |

\*Maximum deflection



Table 4 - continued

Specimen No. 14 Thickness = .1878 inches

| $\begin{array}{c} y \\ x \end{array}$ | -1.0 | -0.5 | 0     | 0.5  | 1.0  |
|---------------------------------------|------|------|-------|------|------|
| -2.0                                  |      |      | .0585 |      |      |
| -1.5                                  |      |      | .107  |      |      |
| -1.0                                  |      |      | .1355 |      |      |
| -0.5                                  |      |      | .149  |      |      |
| 0                                     | .082 | .133 | .158* | .133 | .079 |
| 0.5                                   |      |      | .151  |      |      |
| 1.0                                   |      |      | .136  |      |      |
| 1.5                                   |      |      | .106  |      |      |
| 2.0                                   |      |      | .565  |      |      |

Specimen No. 1 Thickness = .1881 inches

| $\begin{array}{c} y \\ x \end{array}$ | -1.0 | -0.5  | 0     | 0.5   | 1.0  |
|---------------------------------------|------|-------|-------|-------|------|
| -2.0                                  |      |       | .067  |       |      |
| -1.5                                  |      |       | .141  |       |      |
| -1.0                                  |      |       | .172  |       |      |
| -0.5                                  |      |       | .212  |       |      |
| 0                                     | .117 | .2185 | .227* | .2165 | .118 |
| 0.5                                   |      |       | .215  |       |      |
| 1.0                                   |      |       | .211  |       |      |
| 1.5                                   |      |       | .143  |       |      |
| 2.0                                   |      |       | .072  |       |      |

\*Maximum deflection



Table 4 - continued

Specimen No. 16 Thickness = .1884 inches

| $\begin{array}{c} y \\ x \end{array}$ | -1.0 | -0.5 | 0     | 0.5  | 1.0  |
|---------------------------------------|------|------|-------|------|------|
| -2.0                                  |      |      | .185  |      |      |
| -1.5                                  |      |      | .323  |      |      |
| -1.0                                  |      |      | .395  |      |      |
| -0.5                                  |      |      | .436  |      |      |
| 0                                     | .222 | .381 | .454* | .376 | .220 |
| 0.5                                   |      |      | .439  |      |      |
| 1.0                                   |      |      | .396  |      |      |
| 1.5                                   |      |      | .323  |      |      |
| 2.0                                   |      |      | .186  |      |      |

\*Maximum deflection



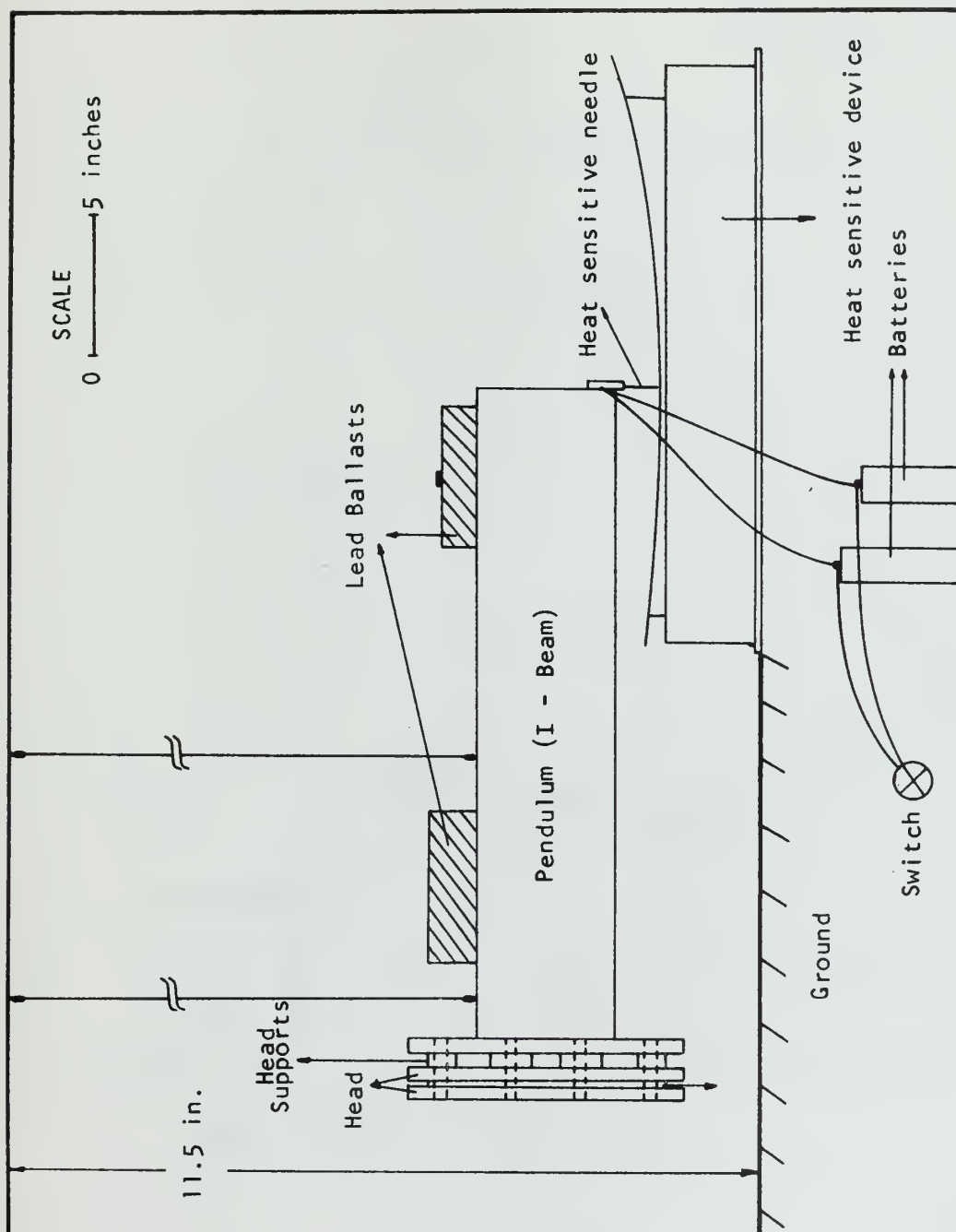


FIGURE I  
THE BALLISTIC PENDULUM





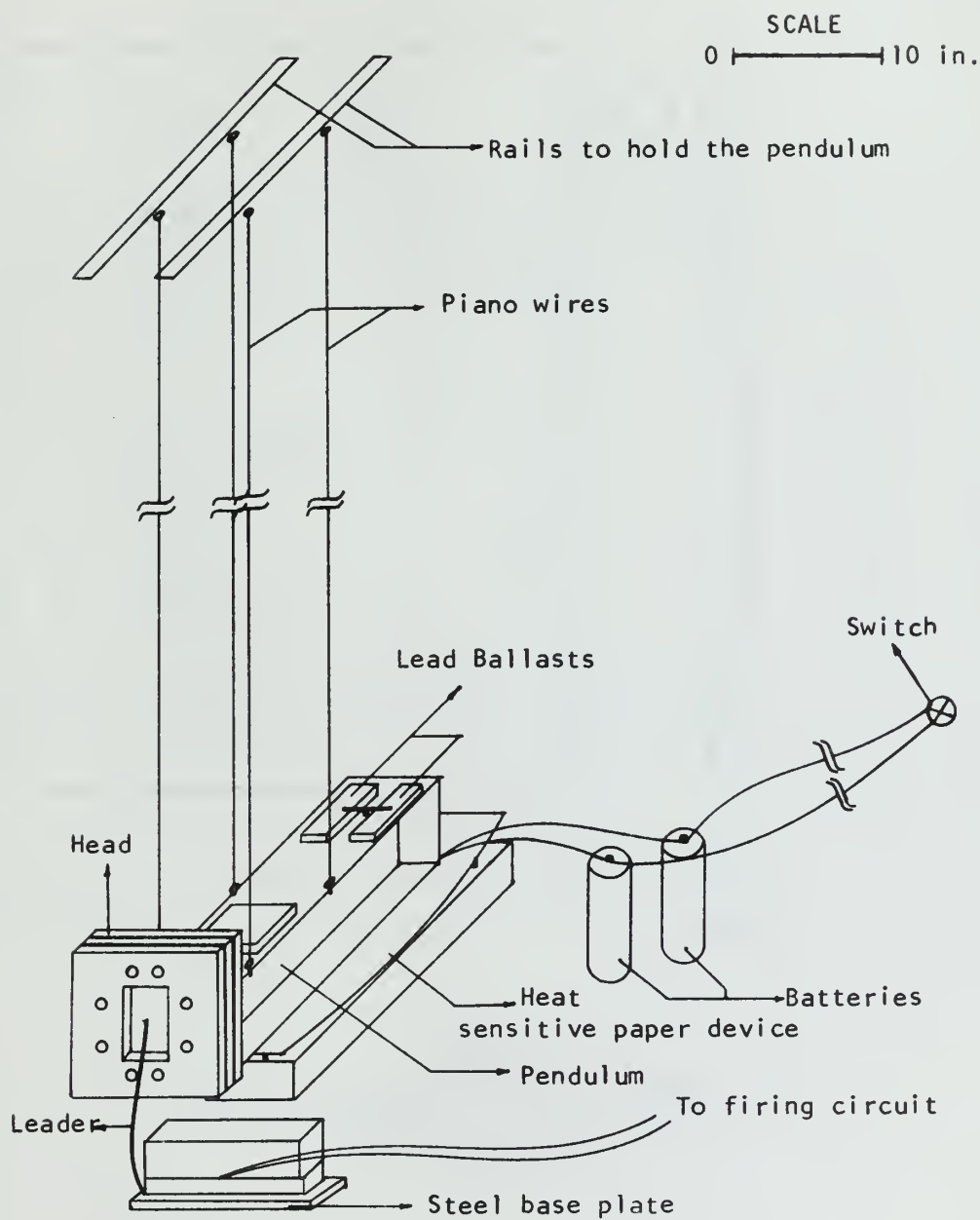


FIGURE 2  
EXPERIMENTAL APPARATUS



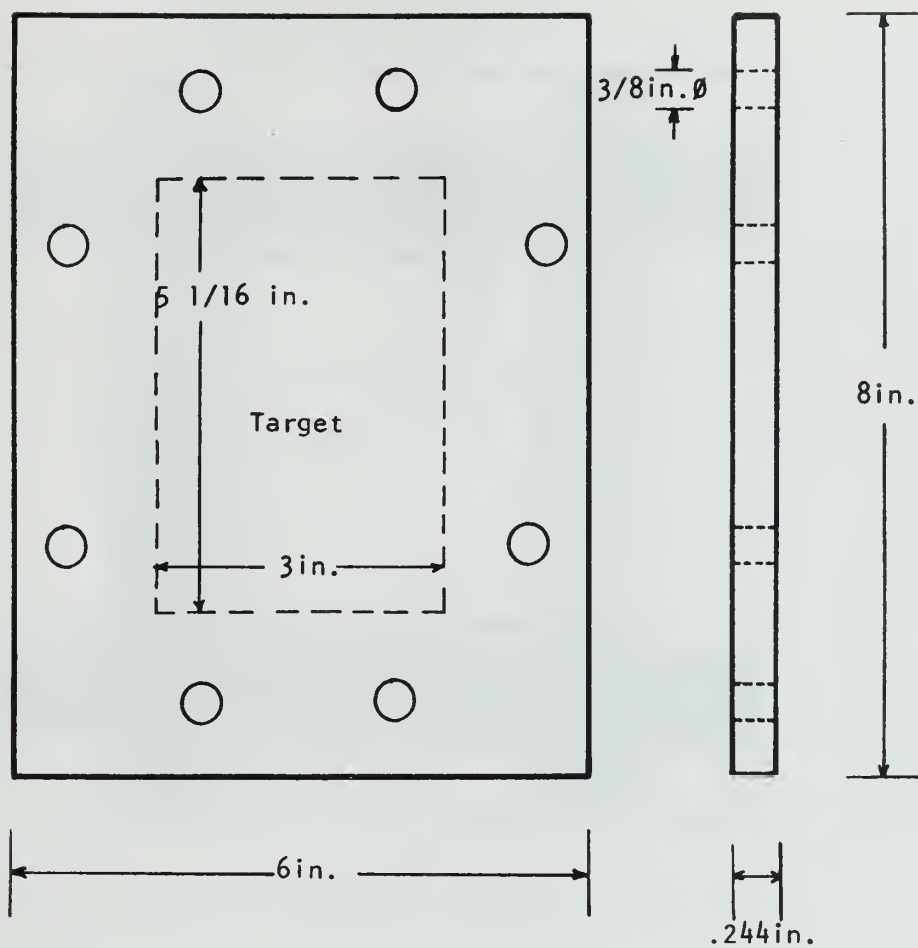


FIGURE 3  
PHYSICAL CHARACTERISTICS OF AL. 6061 - T6  
RECTANGULAR PLATE



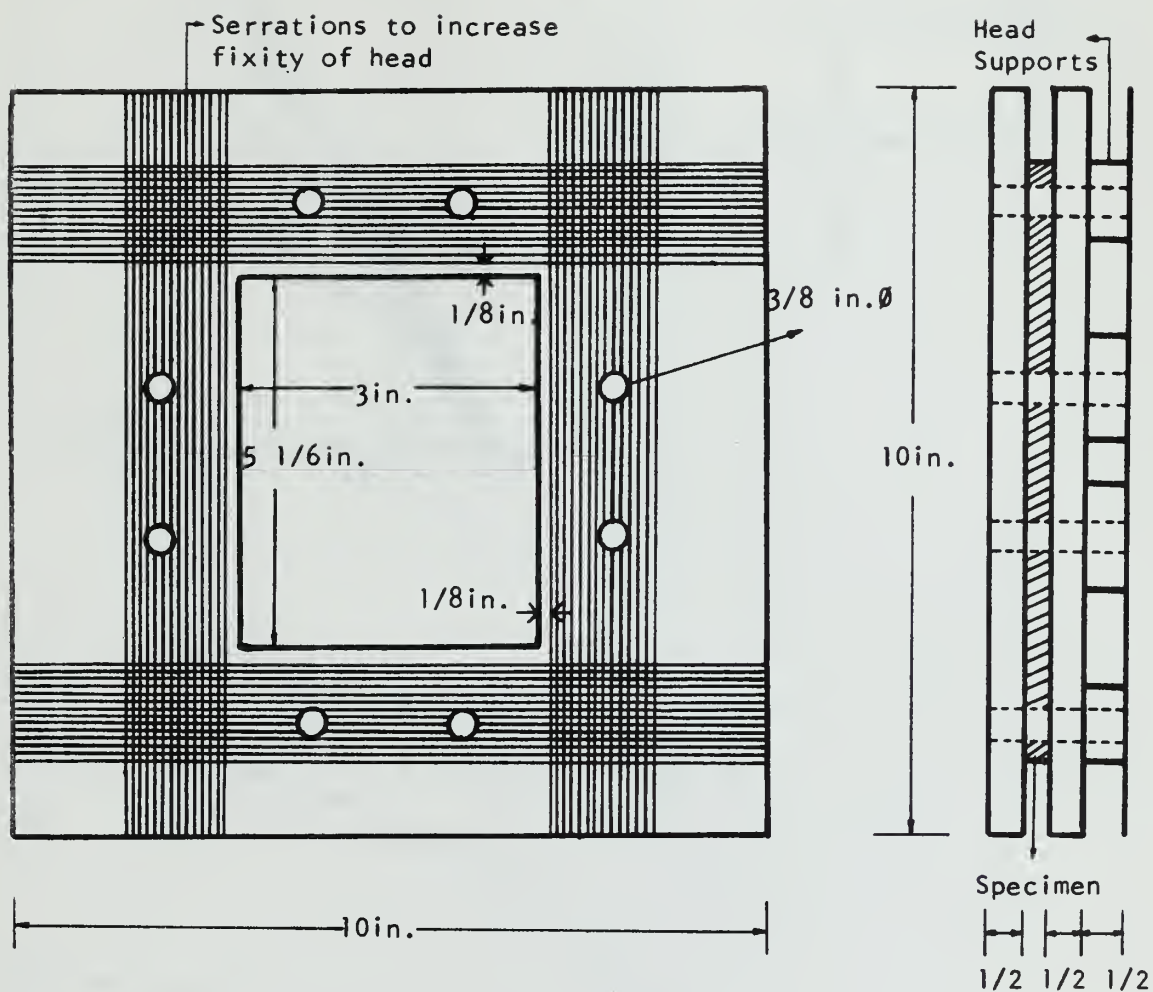


FIGURE 4  
HEAD OF BALLISTIC PENDULUM



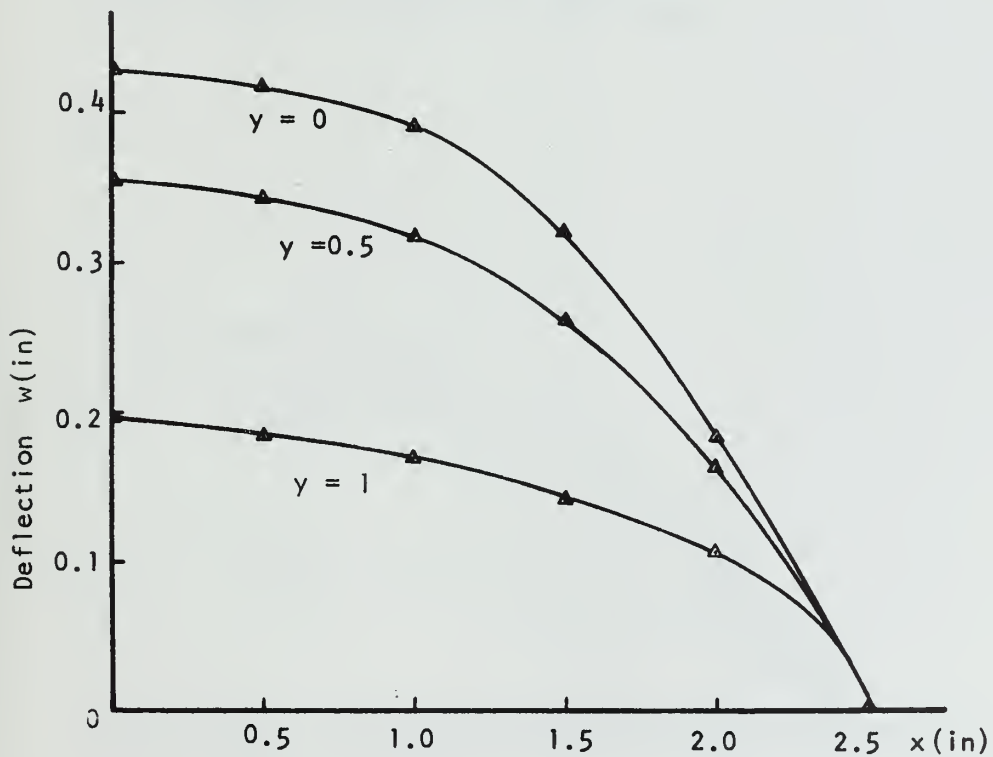
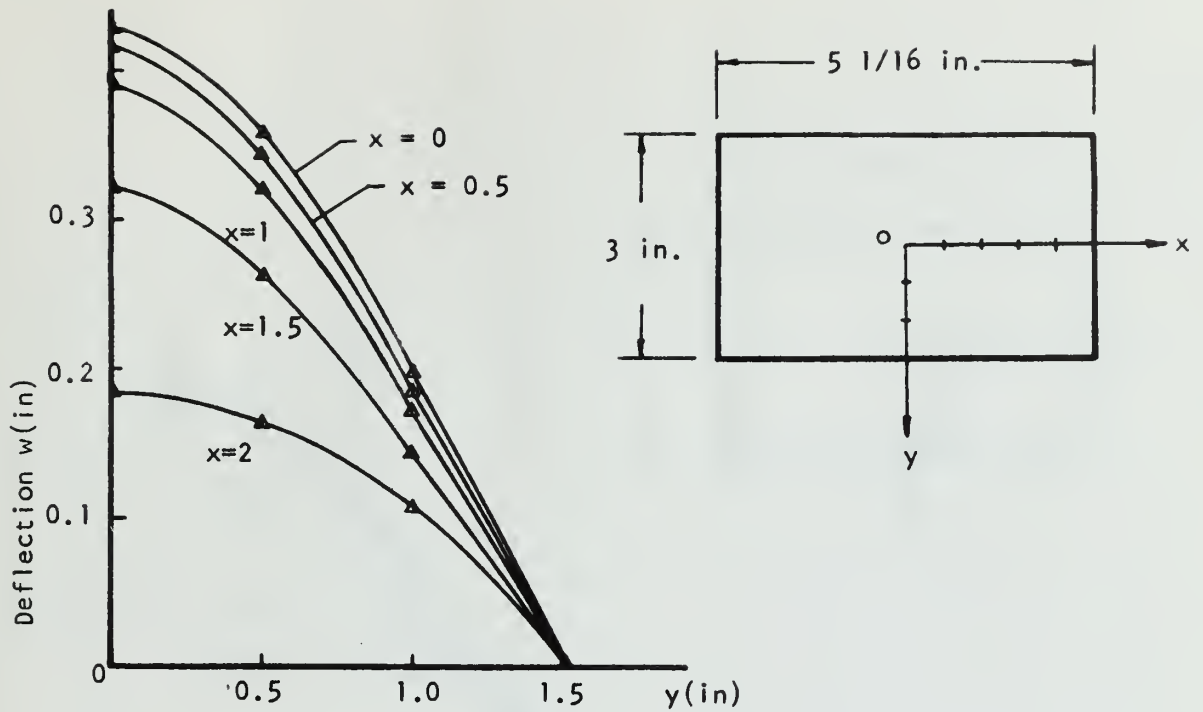


FIGURE 5-A  
 DEFLECTION OF ALUMINUM SPECIMEN NO. 17  
 $H = .1223$





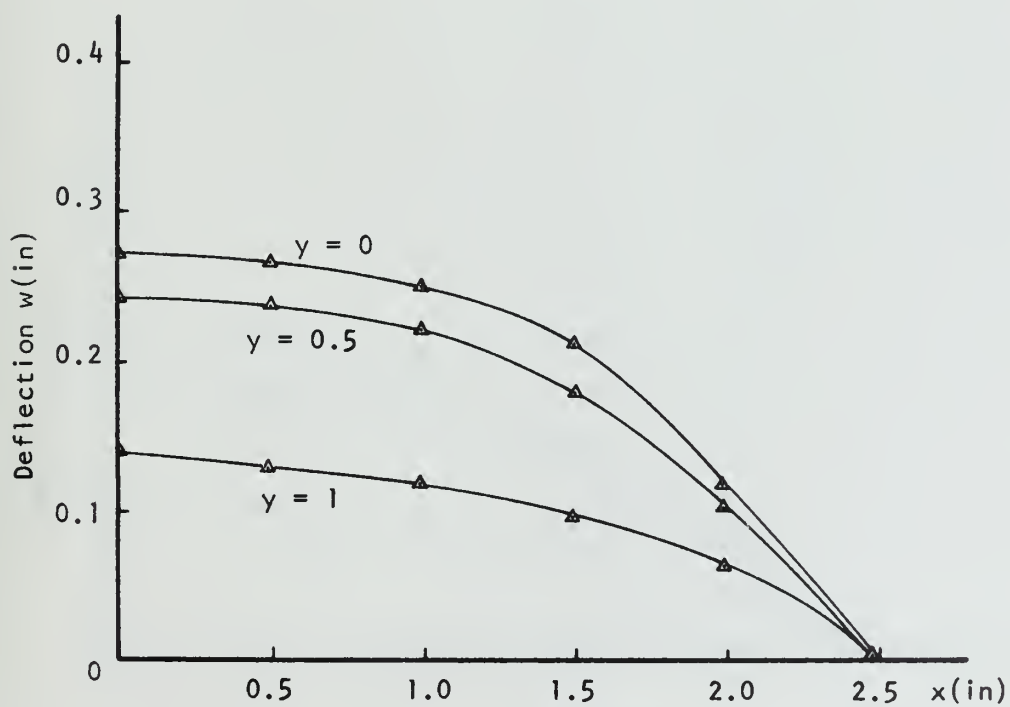
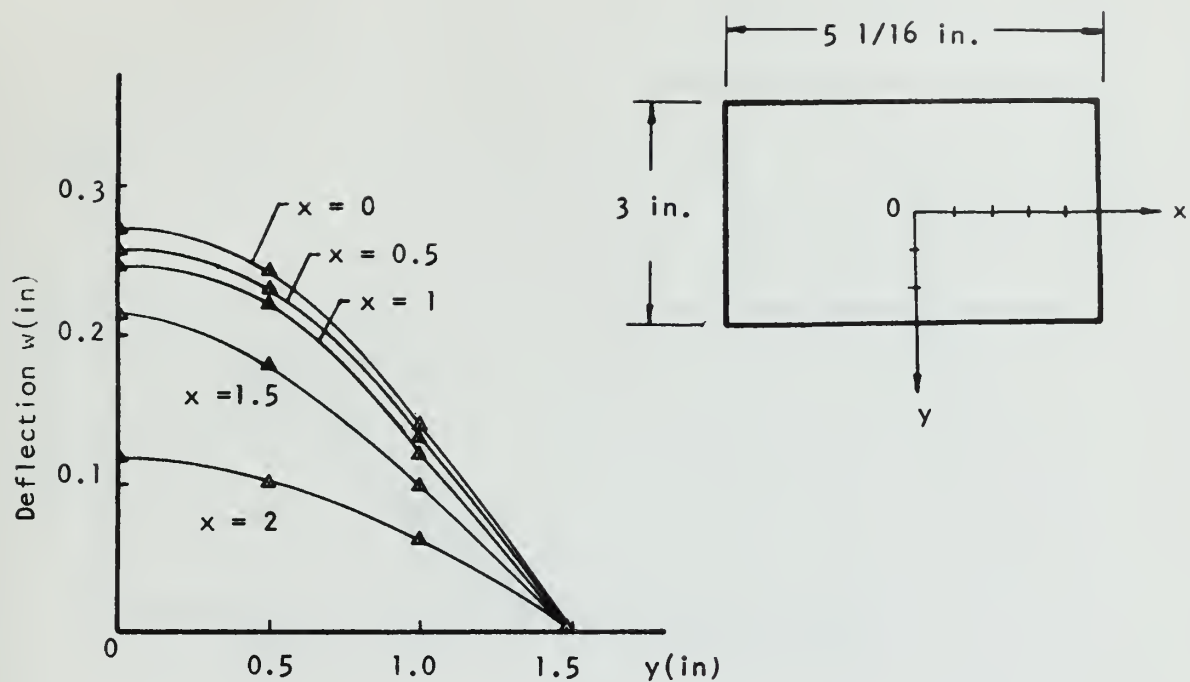


FIGURE 5-B  
 DEFLECTION OF ALUMINUM SPECIMEN NO. 12  
 H - .1221



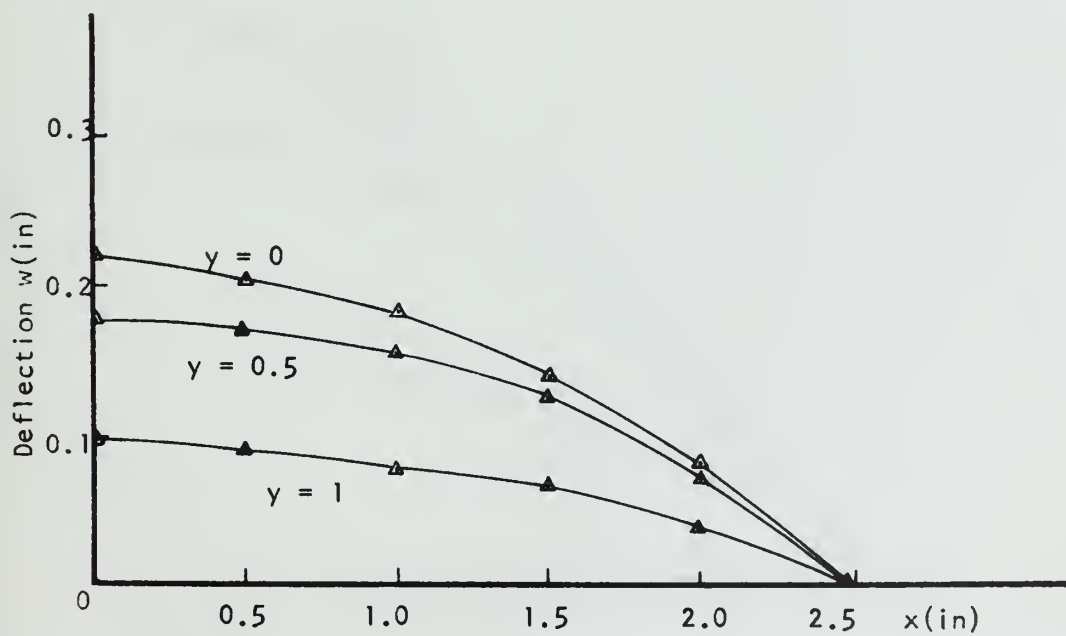
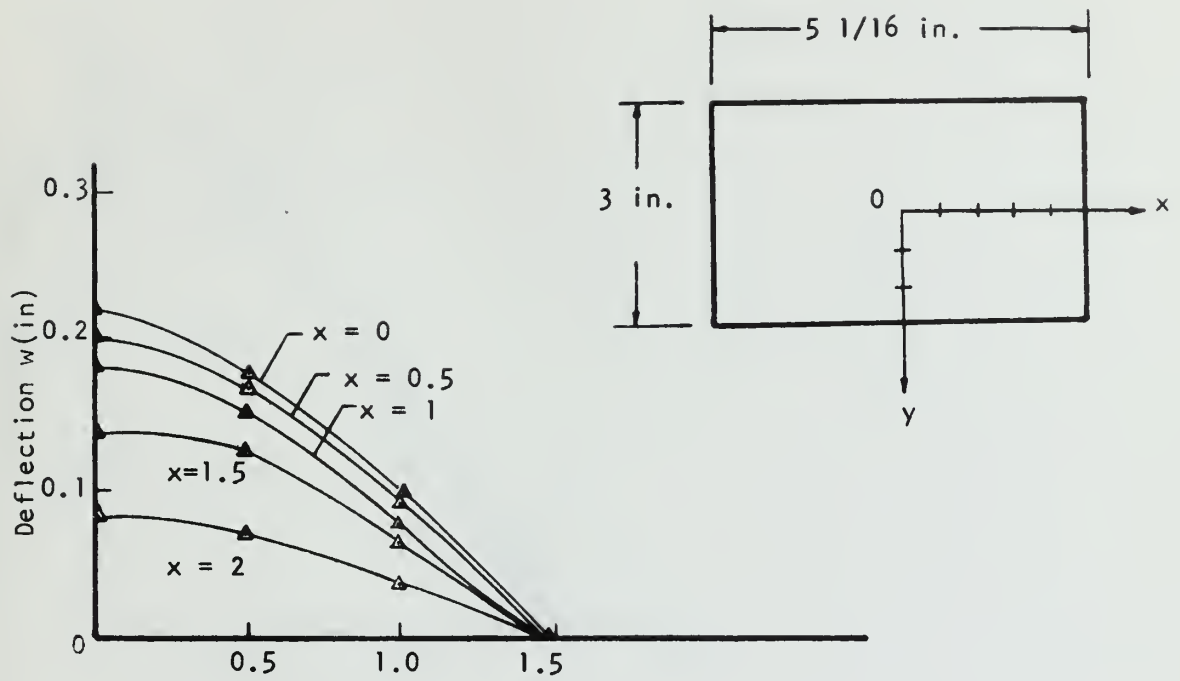


FIGURE 5-c  
DEFLECTION OF ALUMINUM SPECIMEN NO. 15  
 $H = .1228$



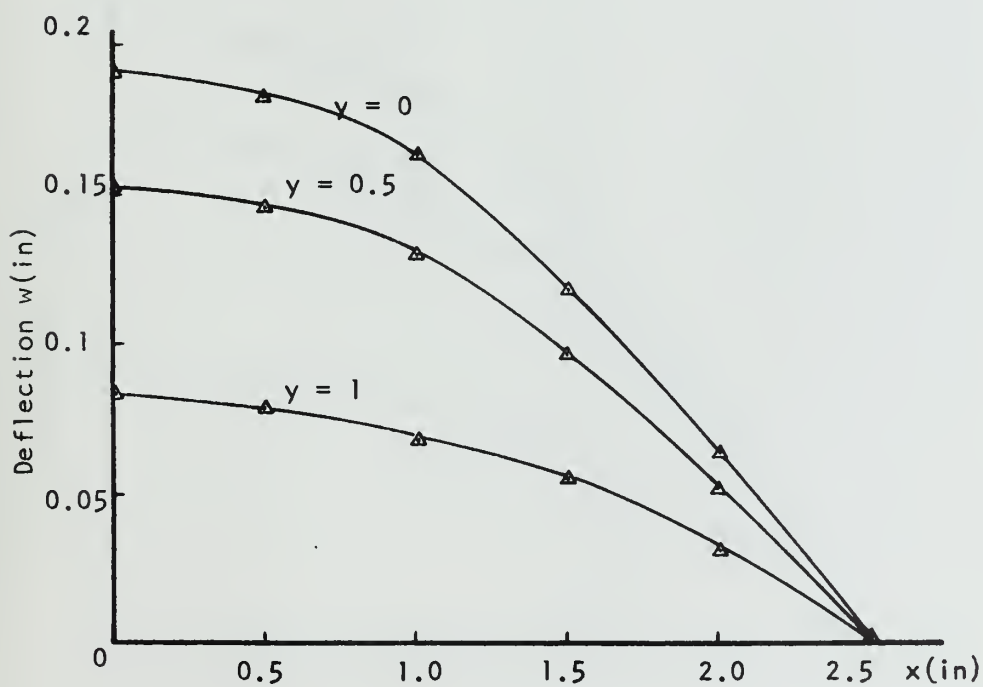
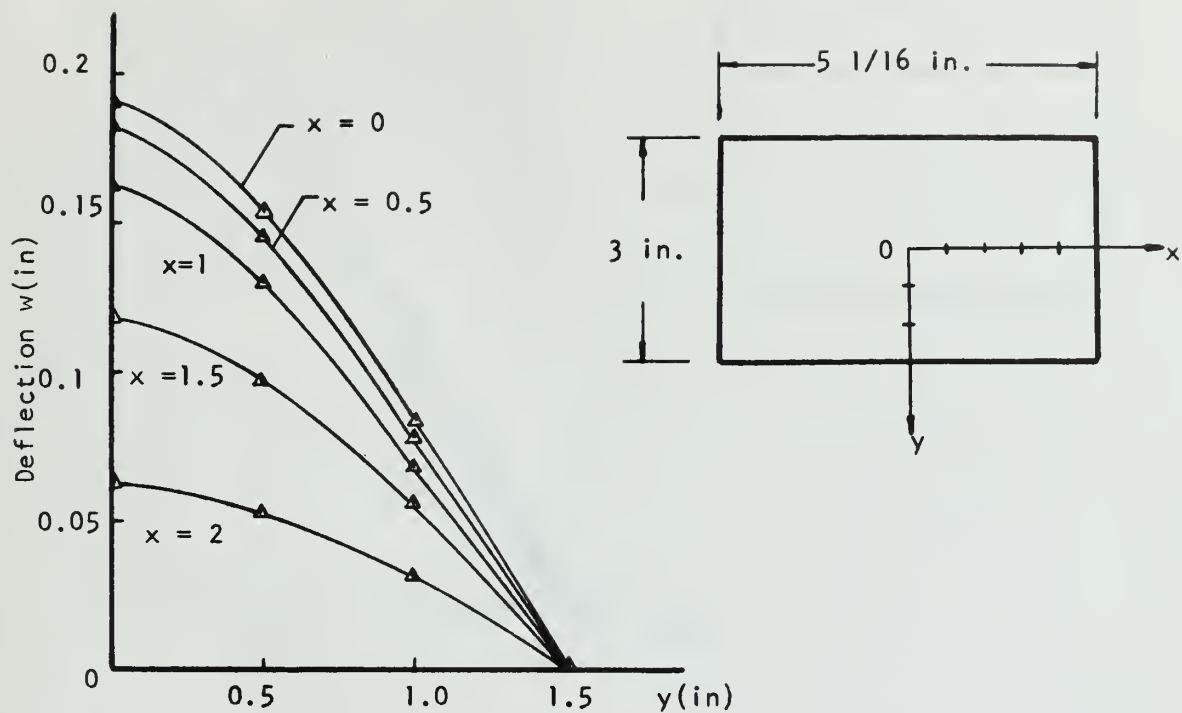


FIGURE 5-D  
 DEFLECTION OF ALUMINUM SPECIMEN NO. 12  
 $H = .1876$



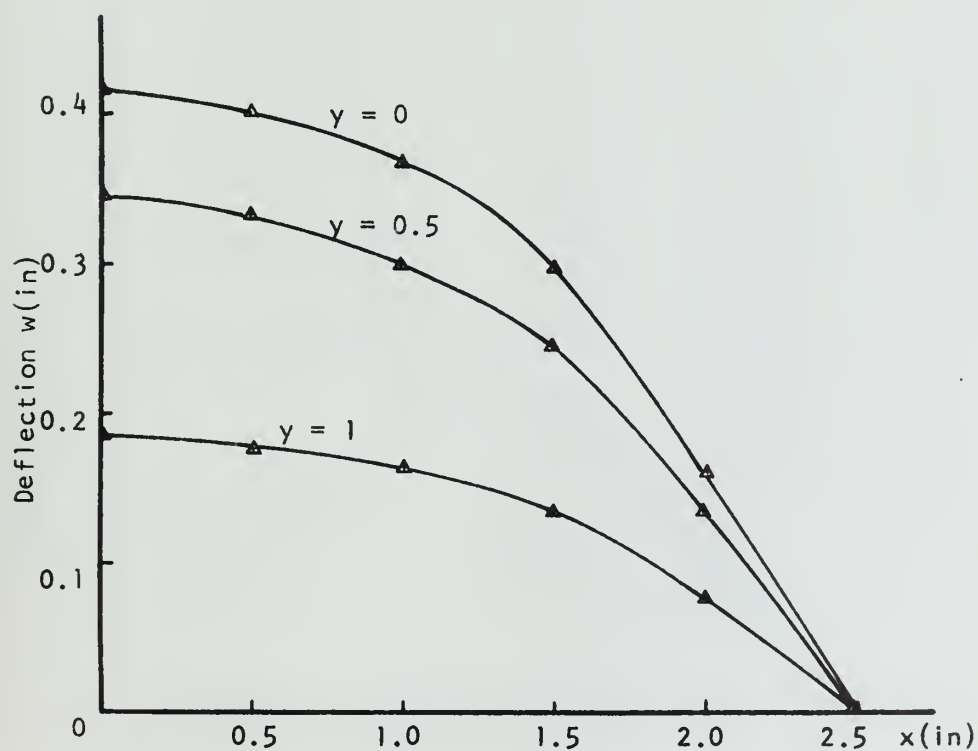
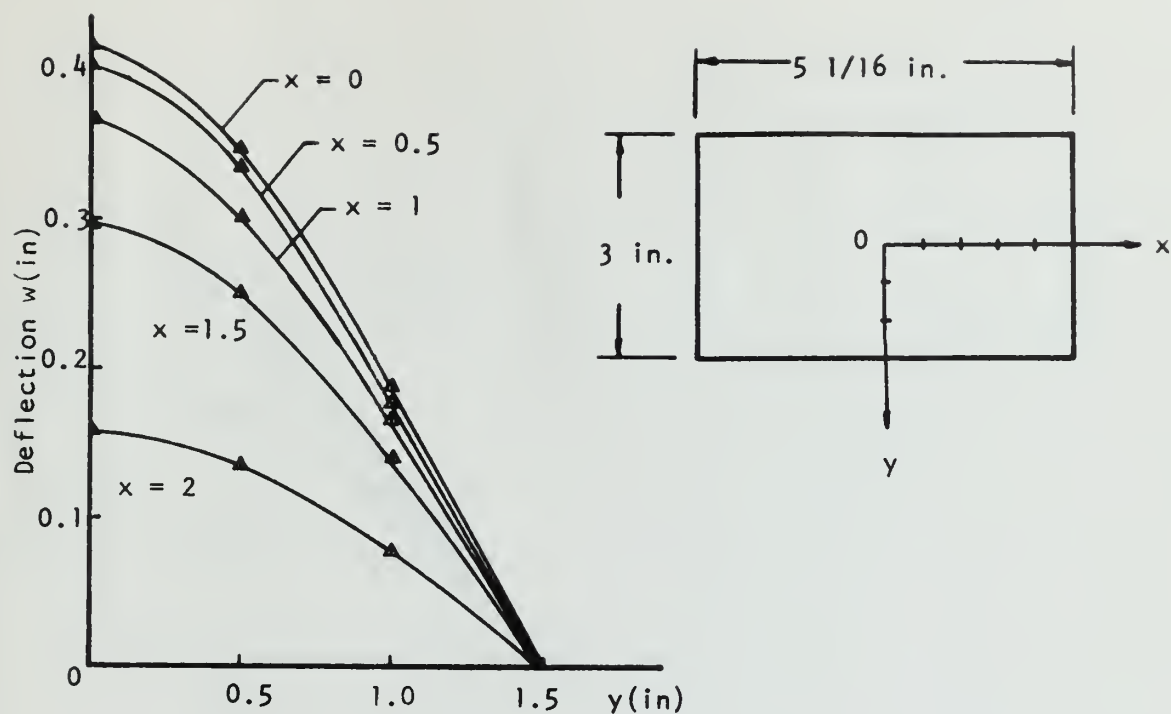


FIGURE 5-E  
 DEFLECTION OF ALUMINUM SPECIMEN NO. 24  
 $H = .18856$





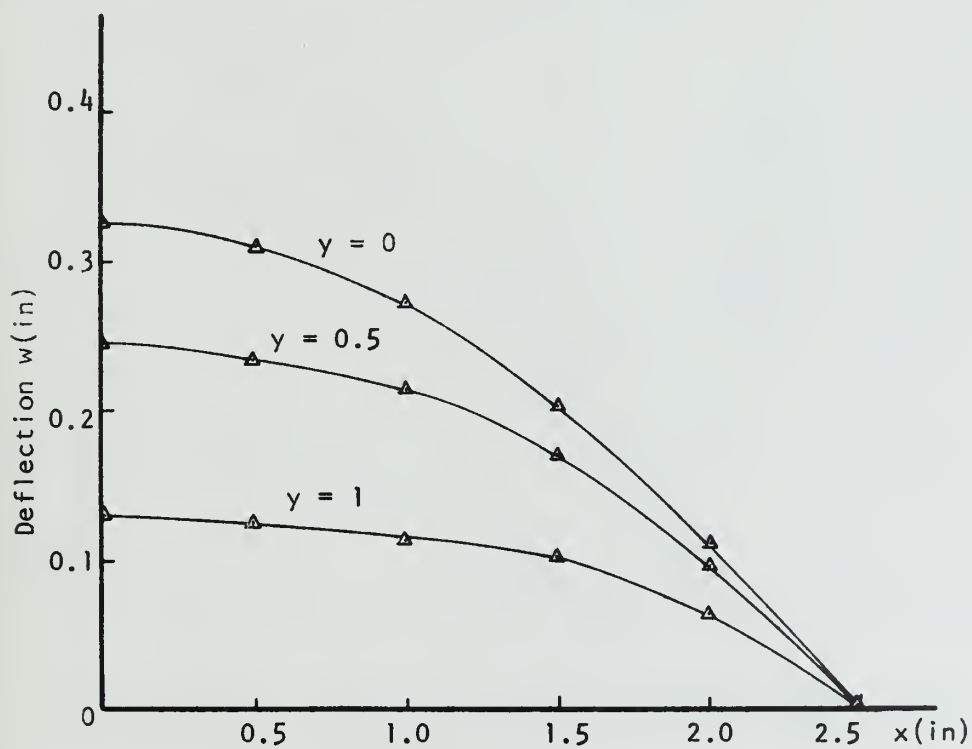
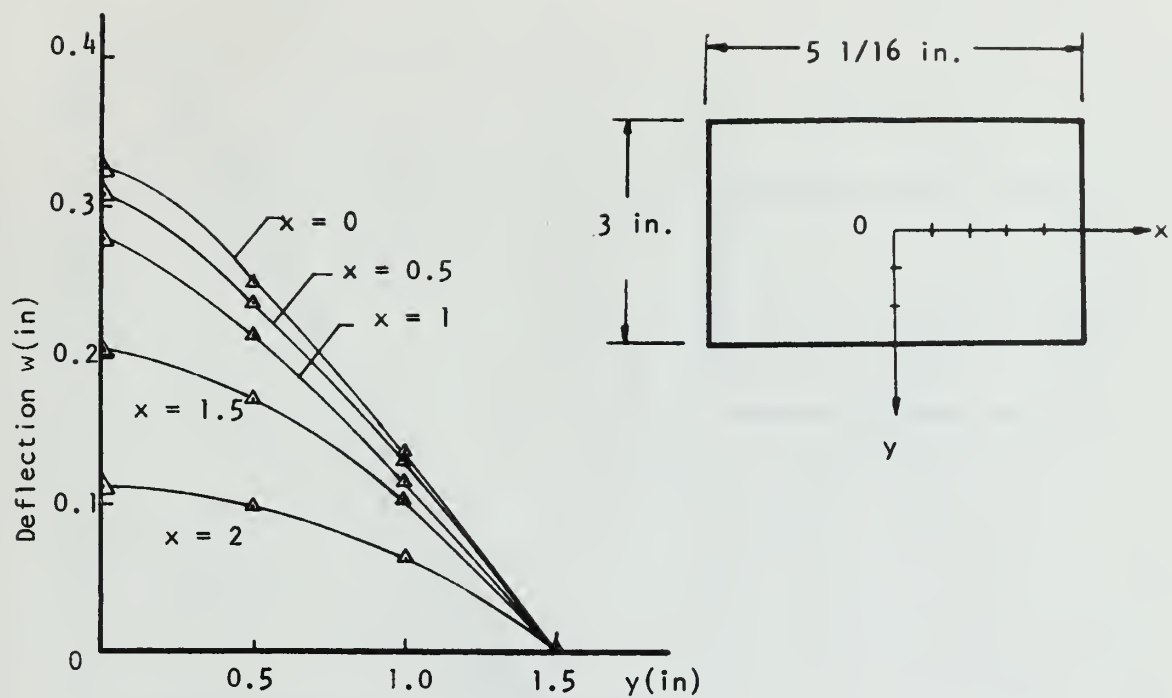


FIGURE 5-F  
 DEFLECTION OF ALUMINUM SPECIMEN NO. 24  
 $H = .2442$



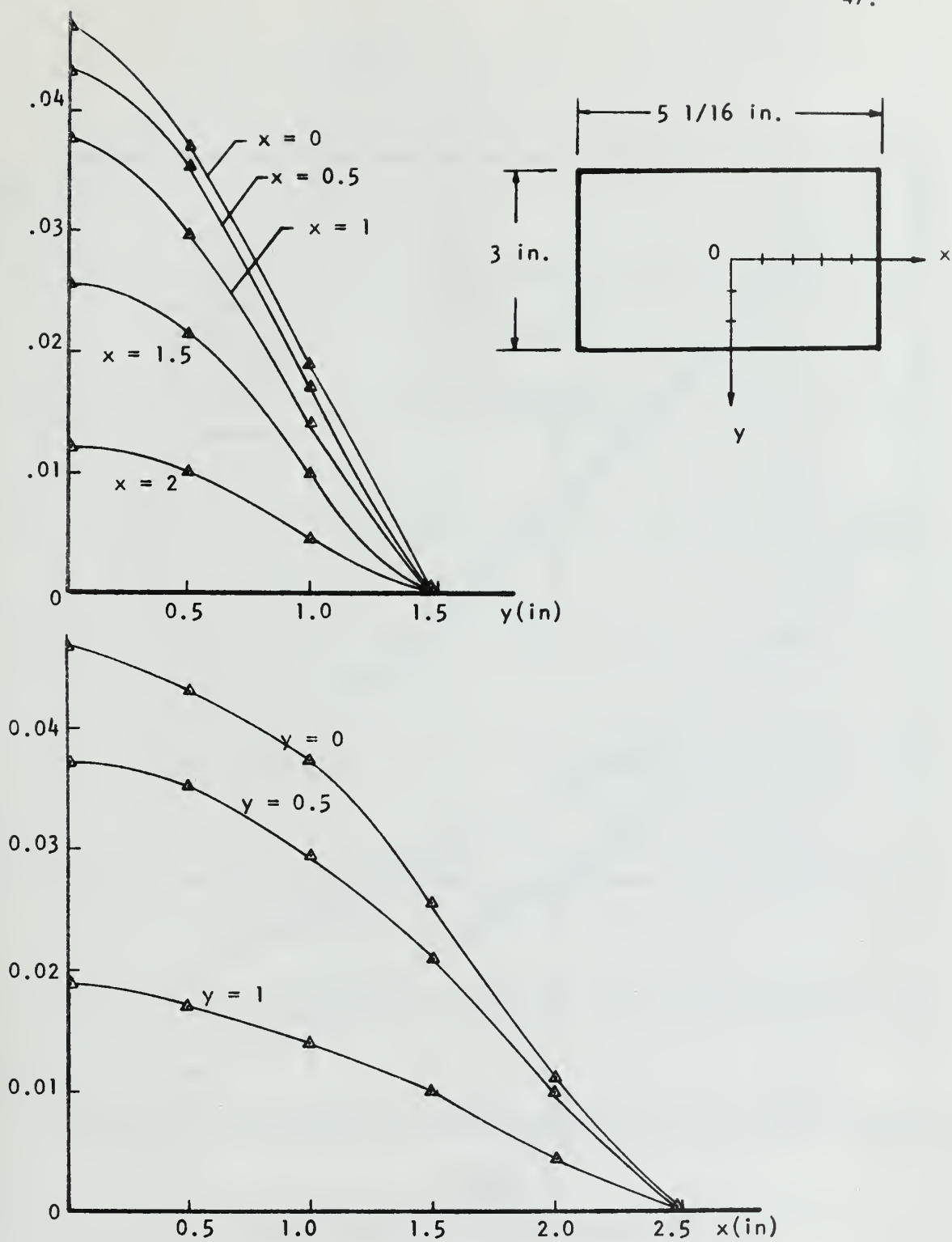


FIGURE 5-G  
DEFLECTION OF ALUMINUM SPECIMEN NO. 2  
 $H = .24446$



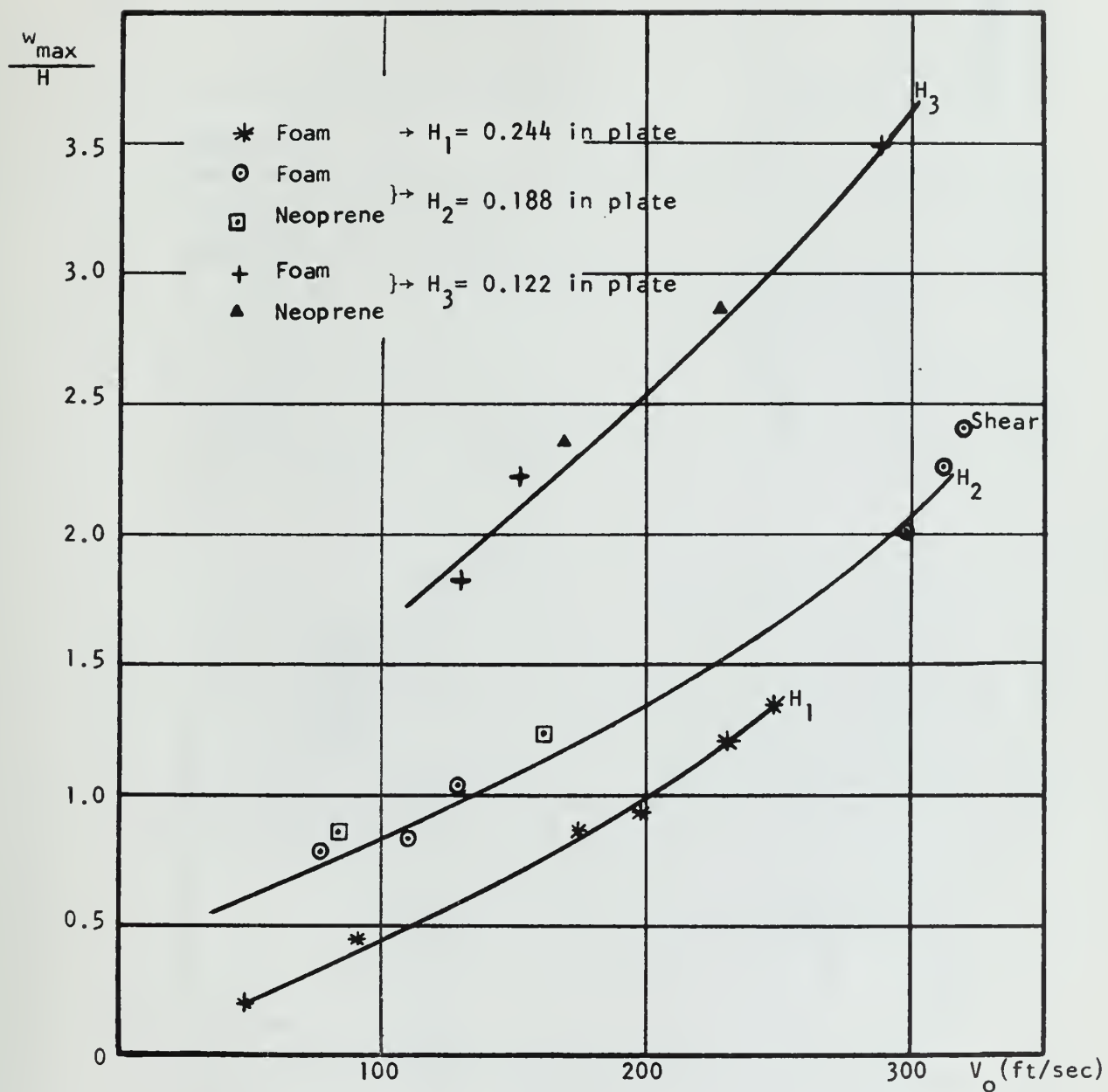
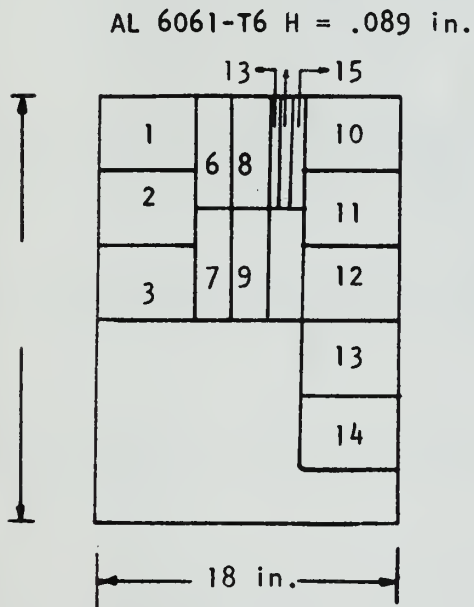
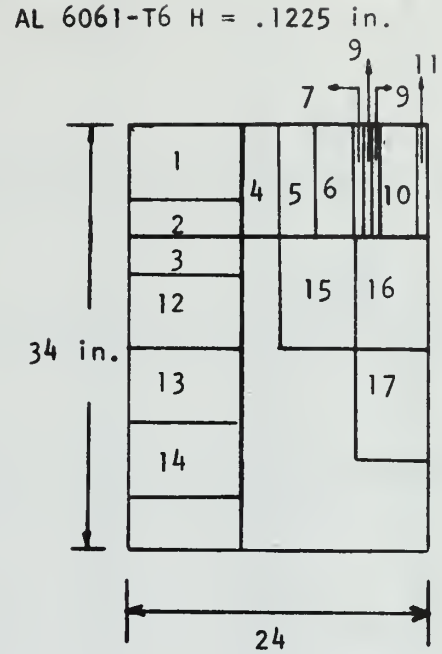
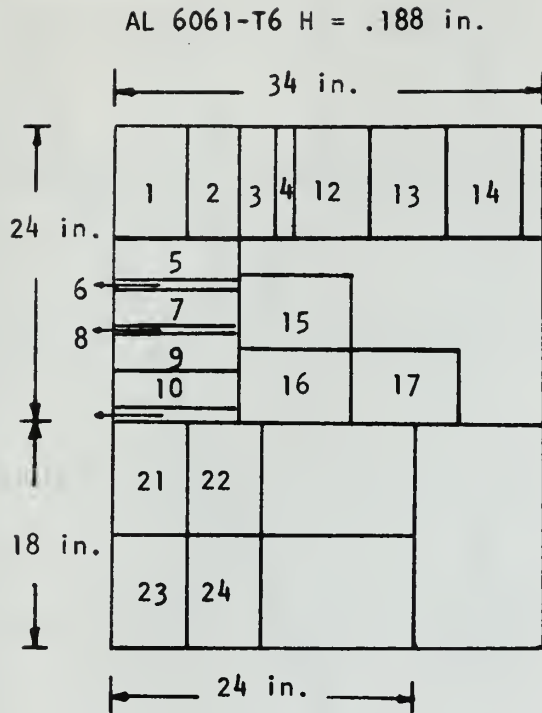


FIGURE 6  
MAXIMUM DEFLECTION - INITIAL VELOCITY RELATIONS





AL 6061-T6 H = .244 in

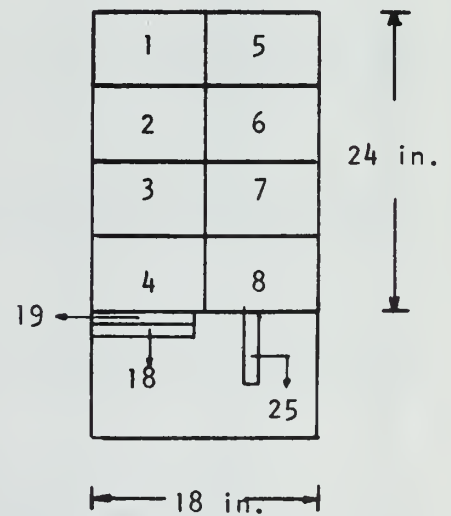


FIGURE 7

LOCATIONS OF SPECIMENS ON ALUMINUM SHEETS





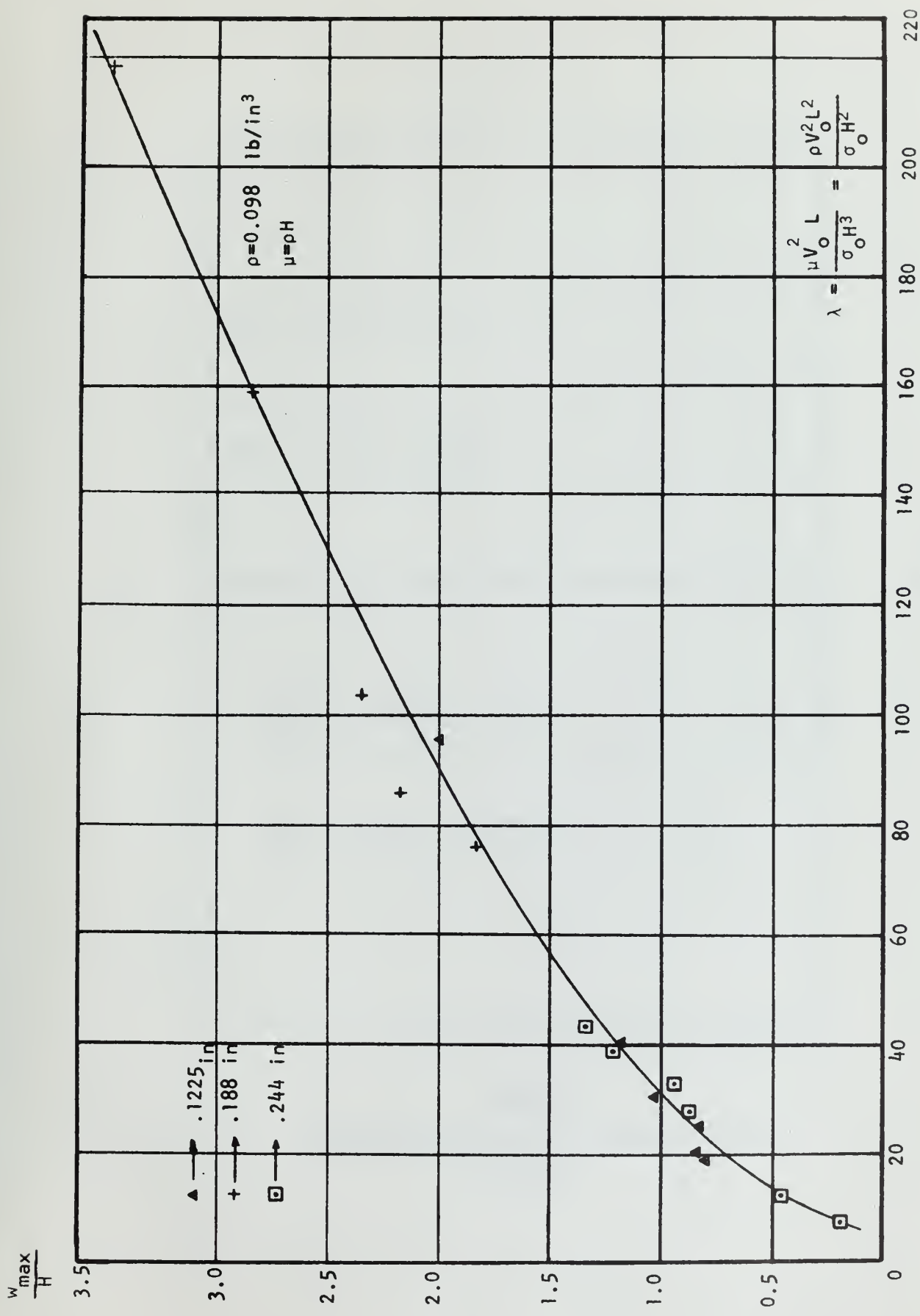


FIGURE 8  
 NONDIMENSIONALIZED RELATION OF  $w_{\max}/H$  VS  $\lambda$



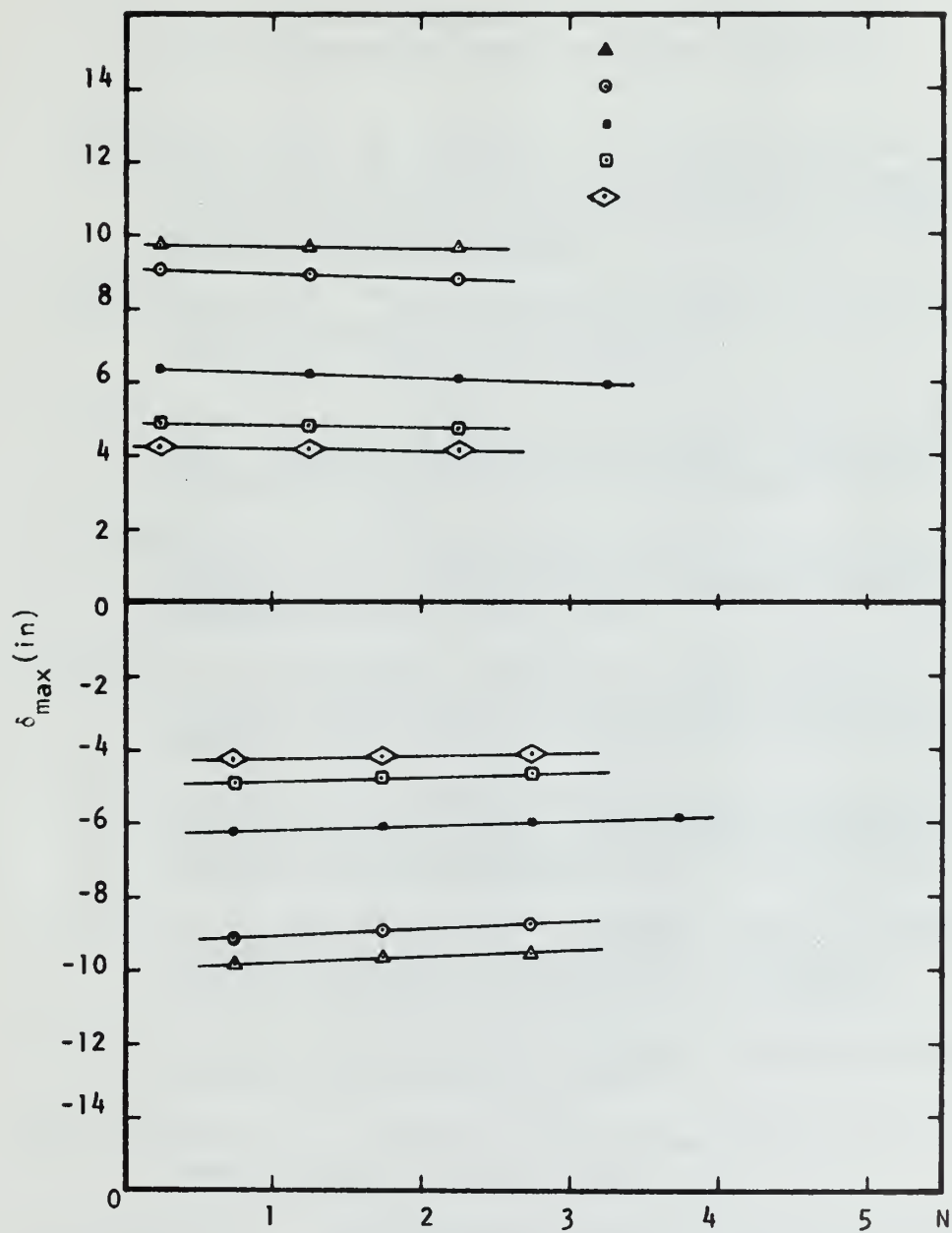


FIGURE 9  
PENDULUM MAXIMUM SWING - NUMBER OF CYCLES  
RELATIONS



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